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Modelling and experimental studies of aerosols and sprays for medical and automotive applications

Multi-component model of droplet heating and evaporation and its implementation into ANSYS Fluent

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Mansour Al Qubeissi, Ahmed Elwardany,
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Outline

- Background
- Mathematical formulation
- Validation
- Conclusions



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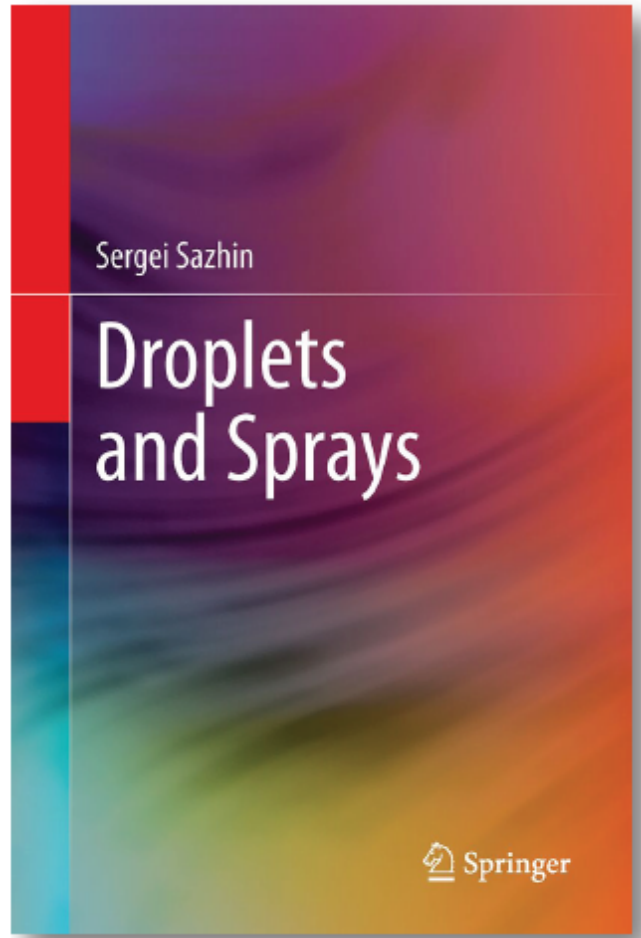
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Types of sprays

Fuel Sprays

Medical Sprays



S. S. Sazhin, Modelling of fuel droplet heating and evaporation: Recent results and unsolved problems, Fuel 196 (2017) 69 – 101.



Background

International Communications in Heat and Mass Transfer 76 (2016) 265–270



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A model for droplet heating and its implementation into ANSYS Fluent



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Mathematical formulation. Temperature

$$c_{pl}m_d \frac{dT}{dt} = 2\pi Nuk_g R_d (T_g - T_s) + L\dot{m}_d + q_{\text{int}}$$

$$\frac{\partial T}{\partial t} = \kappa \left(\frac{\partial^2 T}{\partial R^2} + \frac{2}{R} \frac{\partial T}{\partial R} \right)$$

$$h(T_{\text{eff}} - T_s) = k_l \left. \frac{\partial T}{\partial R} \right|_{R=R_d-0} \quad \kappa = k_l / (c_l \rho_l)$$



Mathematical formulation. Temperature

$$T(r, t) = \frac{1}{r} \sum_{n=1}^{\infty} \left\{ \left(I_n - \frac{R_d \sin \lambda_n}{\lambda_n^2} \zeta(0) \right) \frac{\exp(-\kappa \lambda_n^2 t)}{b_n} - \frac{R_d \sin \lambda_n}{b_n \lambda_n^2} \int_0^t \frac{d\zeta(\tau)}{d\tau} \exp(-\kappa \lambda_n^2 (t - \tau)) d\tau \right\} \sin \left(\lambda_n \frac{r}{R_d} \right) + T_{\text{eff}}(t),$$



Mathematical formulation. Temperature

$$\lambda \cos \lambda + j \sin \lambda = 0$$

$$b_n = \frac{1}{2} \left(1 + \frac{j}{j^2 + \lambda_n^2} \right), \quad I_n = \int_0^{R_d} \frac{r}{R_d} T_0(r) \sin \left(\lambda_n \frac{r}{R_d} \right) dr,$$

$$\kappa = \frac{k_{\text{eff}}}{c_{pl} \rho_l R_d^2}, \quad \zeta(t) = \frac{h T_{\text{eff}}(t) R_d}{k_{\text{eff}}}, \quad T_{\text{eff}} = T_g + \frac{\dot{m}_d L}{2\pi R_d \text{Nu} k_g}$$

$$j = \frac{h R_d}{k_{\text{eff}}} - 1, \quad h = \frac{k_g \text{Nu}}{2 R_d}, \quad k_{\text{eff}} = \chi k_l$$



Mathematical formulation. Temperature

$$\chi = \left(1.86 + 0.86 \tanh \left(2.225 \lg \frac{Pe}{30} \right) \right)$$

$$Pe = 0.79 |\mathbf{v}_g - \mathbf{v}_d| \frac{\mu_g}{\mu_l} \frac{Re_d^{1/3}}{1 + B_M} \frac{\rho_l R_d c_{pl}}{k_l}, \quad Re_d = \frac{2R_d \rho_g |\mathbf{v}_g - \mathbf{v}_d|}{\mu_g}$$

$$B_M = (Y_{vs} - Y_{v\infty}) / (1 - Y_{vs})$$



Mathematical formulation. Temperature

$$\text{Nu} = \frac{\ln(1 + B_T)}{B_T} \text{Nu}^*,$$

$$\text{Nu}^* = 2 + \frac{(1 + \text{Re}_d \text{Pr})^{1/3} \max(1, \text{Re}_d^{0.077}) - 1}{F(B_T)},$$

$$\text{Sh}^* = 2 + \frac{(1 + \text{Re}_d \text{Sc})^{1/3} \max(1, \text{Re}_d^{0.077}) - 1}{F(B_M)},$$

$$F(B_{T,M}) = (1 + B_{T,M})^{0.7} \frac{\ln(1 + B_{T,M})}{B_{T,M}}, \quad B_T = (1 + B_M)^\phi - 1$$

$$\phi = \frac{c_{pv} \rho_g D}{k_g} \frac{\text{Sh}^*}{\text{Nu}^*}, \quad \text{Pr} = \frac{c_{pg} \mu_g}{k_g}, \quad \text{Sc} = \frac{\mu_g}{\rho_g D}.$$



Mathematical formulation. Species diffusion

$$\frac{\partial Y_{li}}{\partial t} = D_l \left(\frac{\partial^2 Y_{li}}{\partial R^2} + \frac{2}{R} \frac{\partial Y_{li}}{\partial R} \right)$$

$$\alpha(\epsilon_i - Y_{lis}) = -D_l \left. \frac{\partial Y_{li}}{\partial R} \right|_{R=R_d-0}$$

$$\alpha = \frac{|\dot{m}_d|}{4\pi\rho_l R_d^2} \quad \epsilon_i = \frac{Y_{vs,i}}{\sum_i Y_{vs,i}}$$



Mathematical formulation. Species diffusion

$$Y_{1,i} = \varepsilon_i + \frac{1}{R} \left\{ \exp \left[D_1 \left(\frac{\lambda_0}{R_d} \right)^2 t \right] [q_{Y_{i0}} - Q_{Y_0} \varepsilon_i] \sinh \left(\lambda_0 \frac{R}{R_d} \right) + \sum_{n=1}^{\infty} \left[\exp \left[-D_1 \left(\frac{\lambda_n}{R_d} \right)^2 t \right] [q_{Y_{in}} - Q_{Y_n} \varepsilon_i] \sin \left(\lambda_n \frac{R}{R_d} \right) \right] \right\},$$

$$\tanh \lambda = -\frac{\lambda}{h_{Y_0}} \quad \text{and} \quad \tan \lambda = -\frac{\lambda}{h_{Y_0}}$$

$$h_{Y_0} = - \left(1 + \frac{\alpha_m R_d}{D_1} \right)$$



Mathematical formulation. Species diffusion

$$Q_{Yn} = \begin{cases} -\frac{1}{\|v_{Y0}\|^2} \left(\frac{R_d}{\lambda_0}\right)^2 (1 + h_{Y0}) \sinh \lambda_0 & \text{when } n = 0 \\ \frac{1}{\|v_{Yn}\|^2} \left(\frac{R_d}{\lambda_n}\right)^2 (1 + h_{Y0}) \sin \lambda_n & \text{when } n \geq 1 \end{cases}$$

$$q_{Yin} = \frac{1}{\|v_{Yn}\|^2} \int_0^{R_d} R Y_{i0}(R) v_{Yn}(R) dR$$

$$v_{Y0}(R) = \sinh \left(\lambda_0 \frac{R}{R_d} \right), \quad v_{Yn}(R) = \sin \left(\lambda_n \frac{R}{R_d} \right), \quad n \geq 1$$



Mathematical formulation. Species diffusion

$$\|v_{Y0}\|^2 = \int_0^{R_d} v_{Y0}^2(R) dR = -\frac{R_d}{2} \left[1 + \frac{h_{Y0}}{h_{Y0}^2 - \lambda_n^2} \right]$$

$$\|v_{Yn}\|^2 = \int_0^{R_d} v_{Yn}^2(R) dR = \frac{R_d}{2} \left[1 + \frac{h_{Y0}}{h_{Y0}^2 + \lambda_n^2} \right], \quad n \geq 1$$

$$D_{\text{eff}} = \chi_Y D_1$$

$$\chi_Y = 1.86 + 0.86 \tanh \left[2.225 \log_{10} \left(\text{Re}_{d(1)} \text{Sc}_1 / 30 \right) \right]$$

$$\text{Sc}_1 = \nu_1 / D_1$$



Validation of the implementation into ANSYS Fluent: Bi-component droplet: acetone+ethanol

| Composition | T_{d0} (K) | d_0 (μm) | T_g (K) | v_d (m/s) |
|----------------|--------------|-------------------------|-----------|-------------|
| 25% ethanol | 305.65 | 133.8 | 294.25 | 12.75 |
| 50% ethanol | 310.65 | 142.7 | 293.95 | 12.71 |
| 75% ethanol | 311.75 | 137.1 | 294.75 | 12.28 |

A. E. Elwardany, I. G. Gusev, G. Castanet, F. Lemoine, S. S. Sazhin, Mono- and multi-component droplet cooling/heating and evaporation: Comparative analysis of numerical models, *Atomization and Sprays* 21 (11) (2011) 907–931.



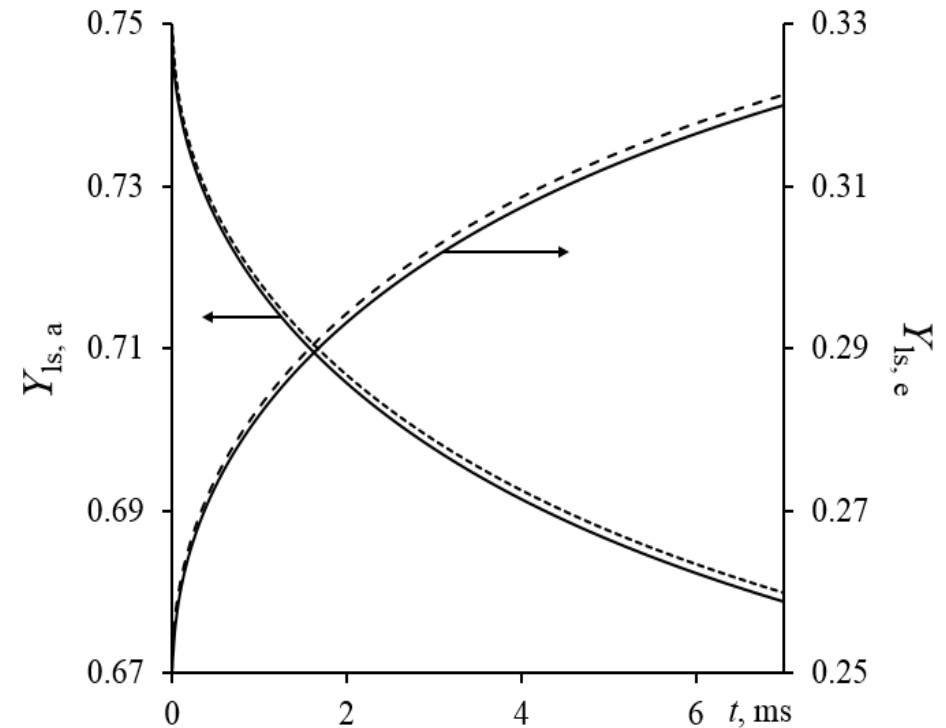
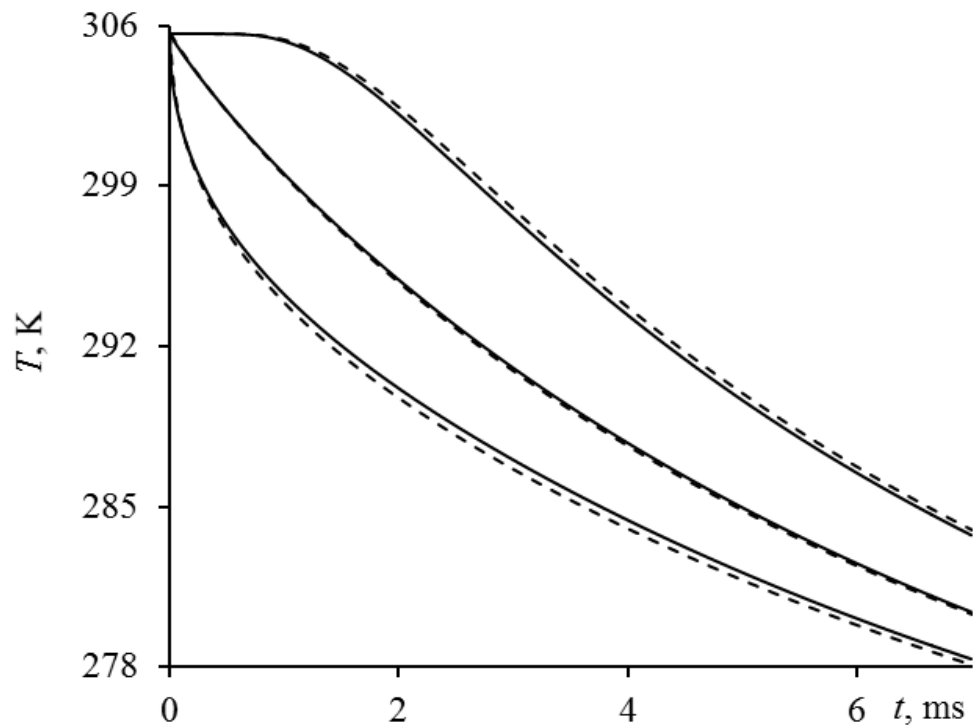
Validation of the implementation into ANSYS Fluent: Bi-component droplet: acetone+ethanol

| Composition | Error (T_d) | Error ($Y_{ls,e}$) | Error ($Y_{ls,a}$) |
|----------------|-----------------|----------------------|----------------------|
| 25% ethanol | 0.1636% | 0.3647% | 0.1726% |
| 50% ethanol | 0.1423% | 0.1730% | 0.3110% |
| 75% ethanol | 0.1294% | 0.2759% | 0.7933% |

A. E. Elwardany, I. G. Gusev, G. Castanet, F. Lemoine, S. S. Sazhin, Mono- and multi-component droplet cooling/heating and evaporation: Comparative analysis of numerical models, *Atomization and Sprays* 21 (11) (2011) 907–931.



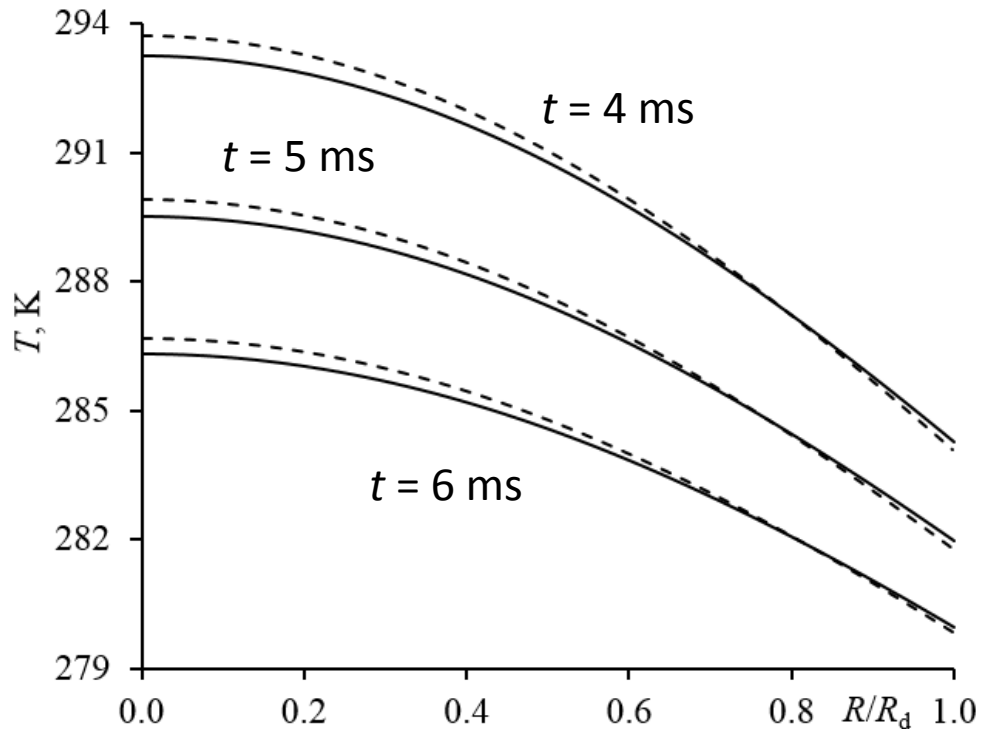
Validation of the implementation into ANSYS Fluent: Bi-component droplet: acetone+ethanol



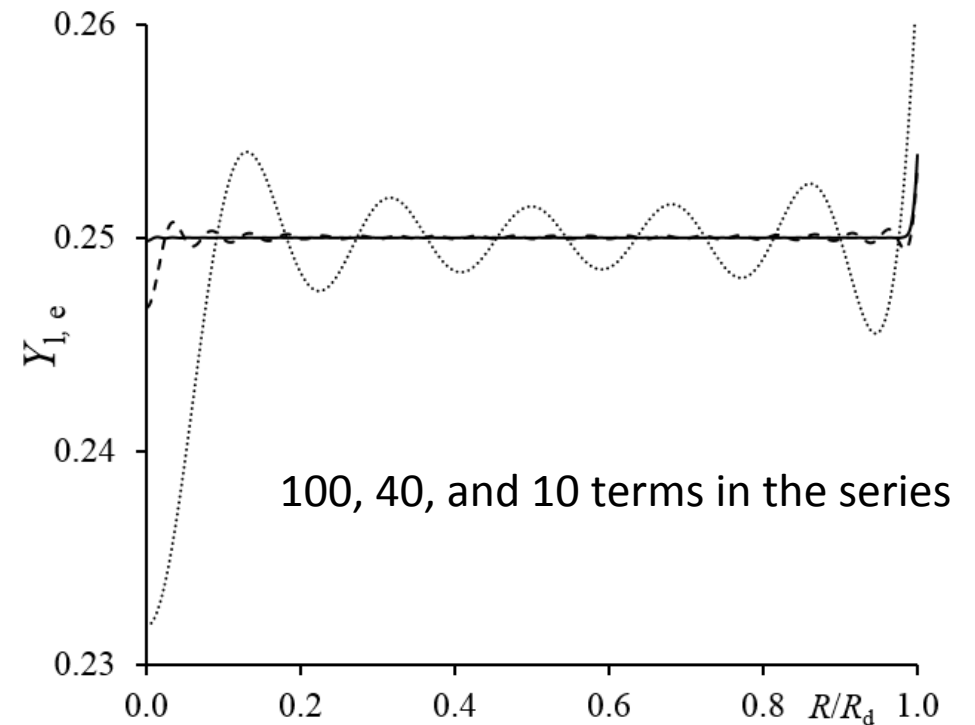
25% ethanol/75% acetone



Validation of the implementation into ANSYS Fluent: Bi-component droplet: acetone+ethanol



25% ethanol/75% acetone



$t = 10^{-5} \text{ s}$



Conclusion

- A model for heating and evaporation of multi-component droplets, based on analytical solutions to the heat transfer and species diffusion equations in the liquid phase, has been summarised.
- The model was implemented into ANSYS Fluent via User-Defined Function (UDF).
- The model was applied to the analysis of the mixtures of acetone/ethanol droplet heating/cooling and evaporation.
- The predictions of the customised version of ANSYS Fluent, with the new model implemented into it, are verified against the results predicted by the previously developed one-dimensional in-house



Acknowledgements

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