



ZHEJIANG
UNIVERSITY



PURDUE
UNIVERSITY

Spatial-temporal measurement of fragments and ligaments in secondary atomization via high-speed DIH

Longchao Yao ^{a, b}, Xuecheng Wu ^a, Jun Chen ^b, Paul E. Sojka ^b, Yingchun Wu ^a

^a *State Key Laboratory of Clean Energy Utilization, Zhejiang University, Hangzhou, 310027 China*

^b *School of Mechanical Engineering, Purdue University, West Lafayette 47907 USA*

Presenter: Yingchun Wu

7 August, 2018

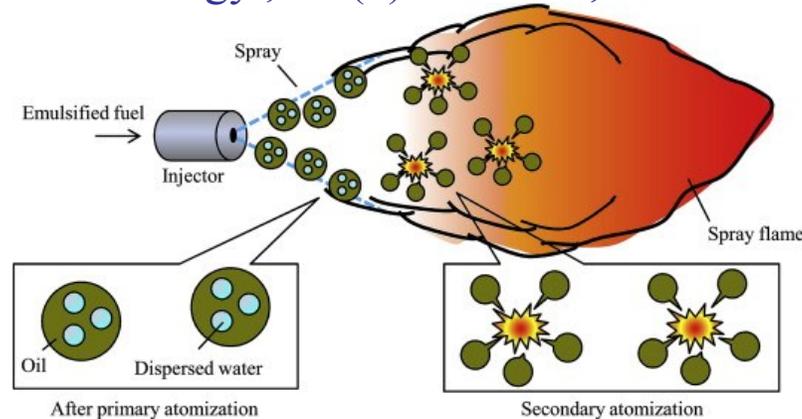
Background

Liquid atomization has wide applications in liquid fuel combustion, agriculture spray, food processing, etc. Secondary atomization determines the final size and velocity.

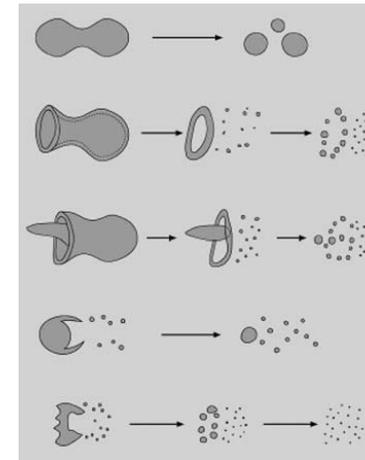
Energy , 35 (2) :806-813, 2010



Spray in engine



Secondary atomization



Breakup regimes

Vibrational, $We < \sim 11$

Bag, $\sim 11 < We < \sim 35$

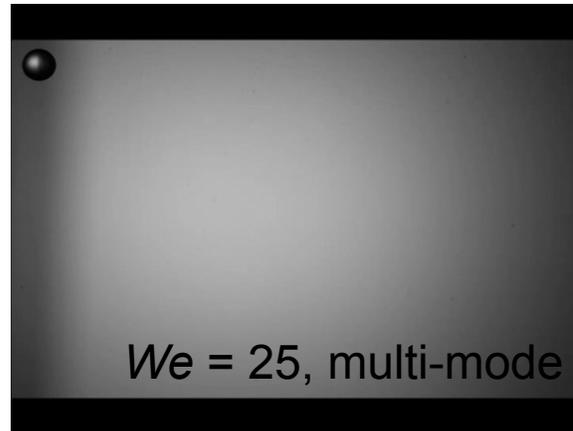
Multimode, $\sim 35 < We < \sim 80$

Shearing, $\sim 80 < We < \sim 350$

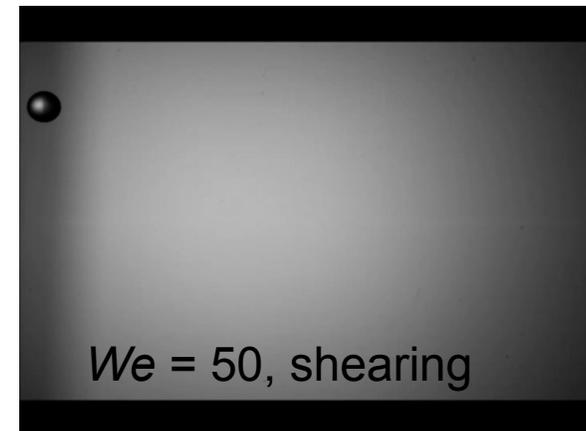
Catastrophic, $We > \sim 350$



$We = 13$, bag



$We = 25$, multi-mode

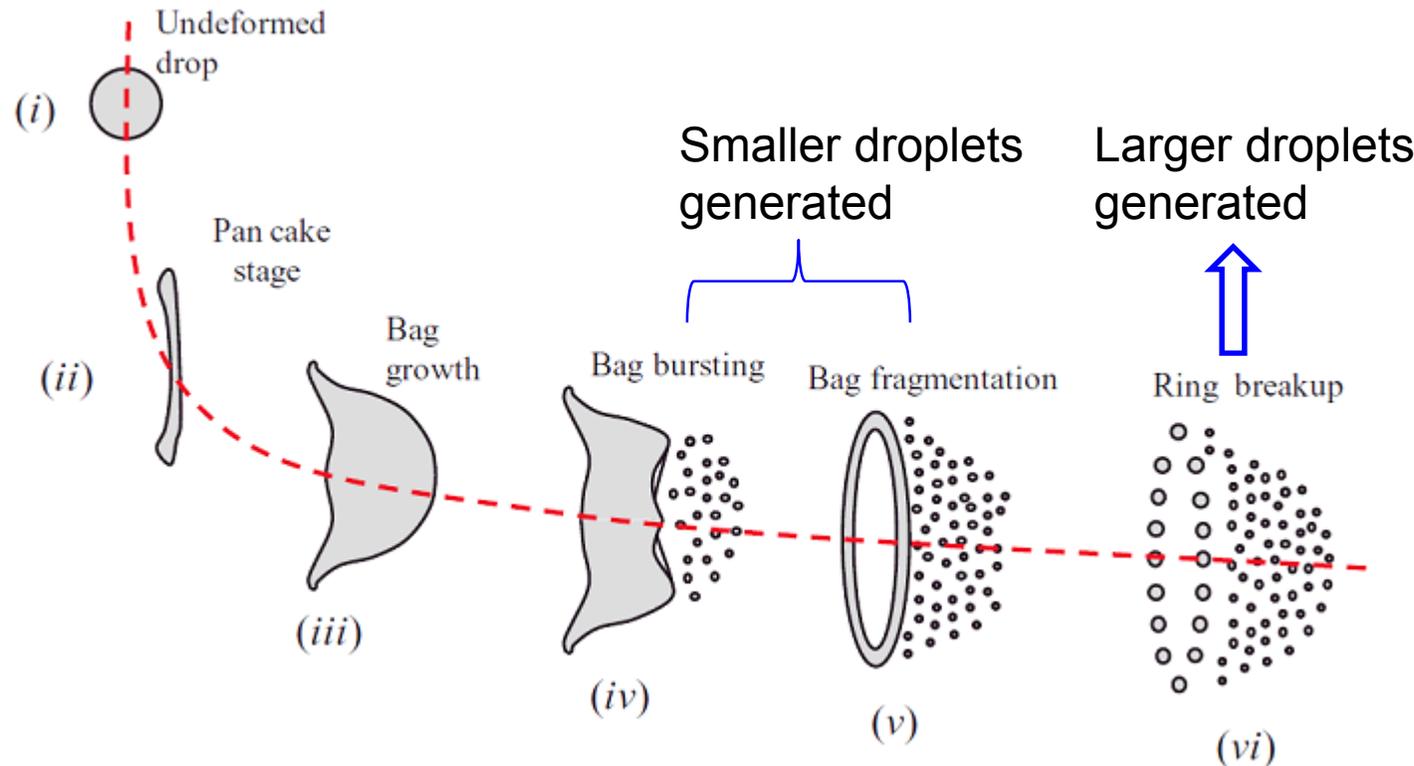


$We = 50$, shearing

(videos)

Motivation

- Quantify 3D fragments and ligaments and their evolution in during secondary atomization.



Phys. Fluids 26, 072103 (2014)

- In bag and multi-mode (bag-stamen) breakup

- Establish onset of secondary atomization
- Two stages: bag rupture and rim disintegration
- Droplet size and velocity are important parameters
- Complicated 3D rim

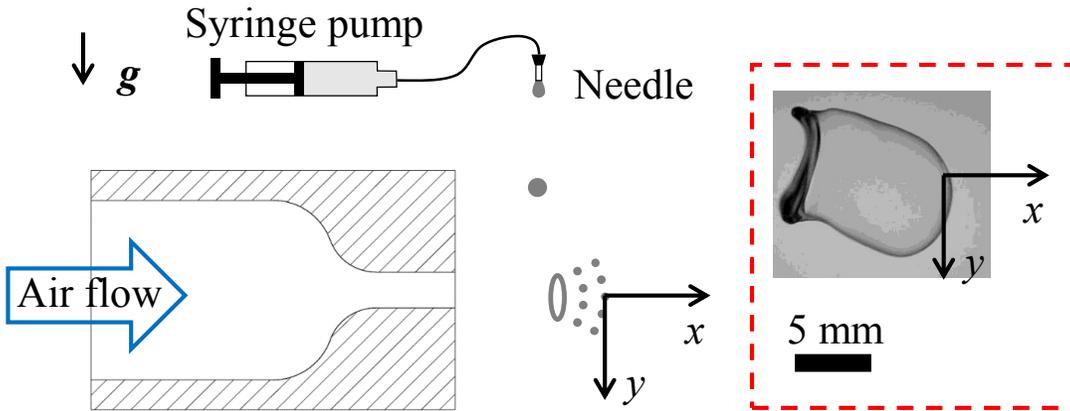
$$\text{Weber number: } We = \frac{\rho_g u_0^2 d_0}{\sigma},$$

ρ_g – gas density u_0 – relative velocity

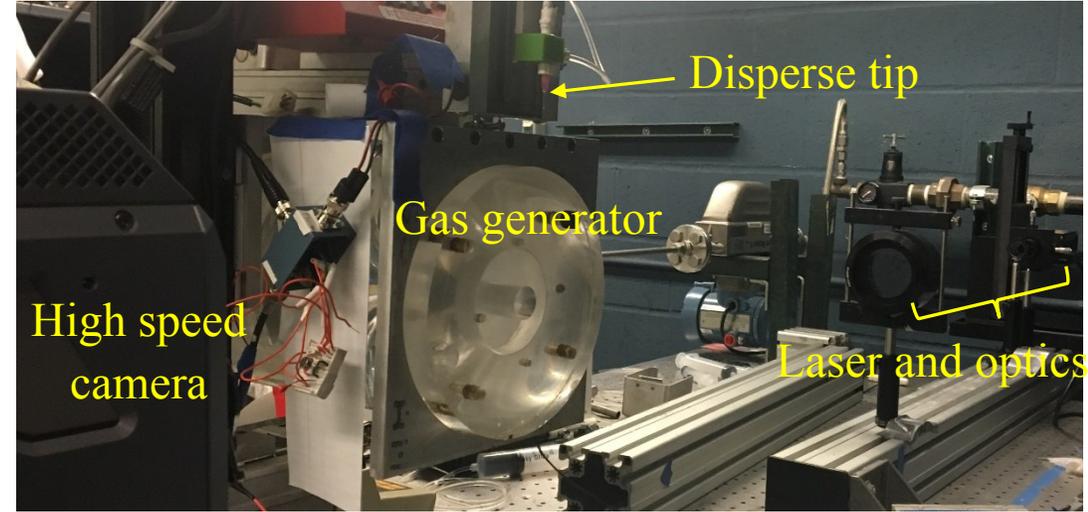
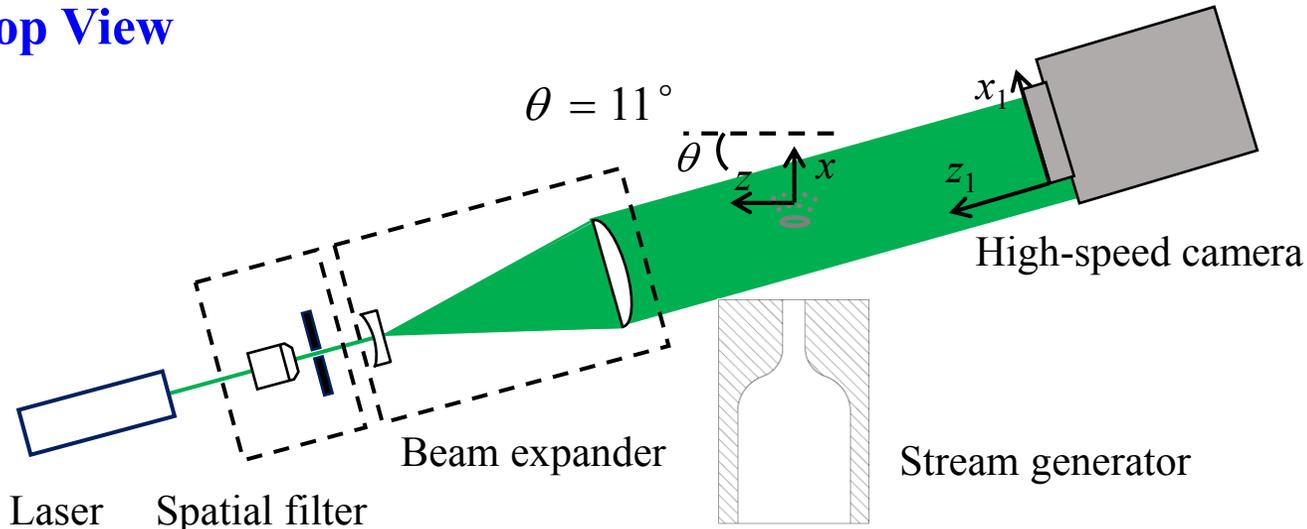
d_0 – drop diameter σ – surface tension

Experimental setup

Side View



Top View



- A tilted illumination to reduce overlap
- Use the bag burst point as start of time t_0 and origin of coordinates.

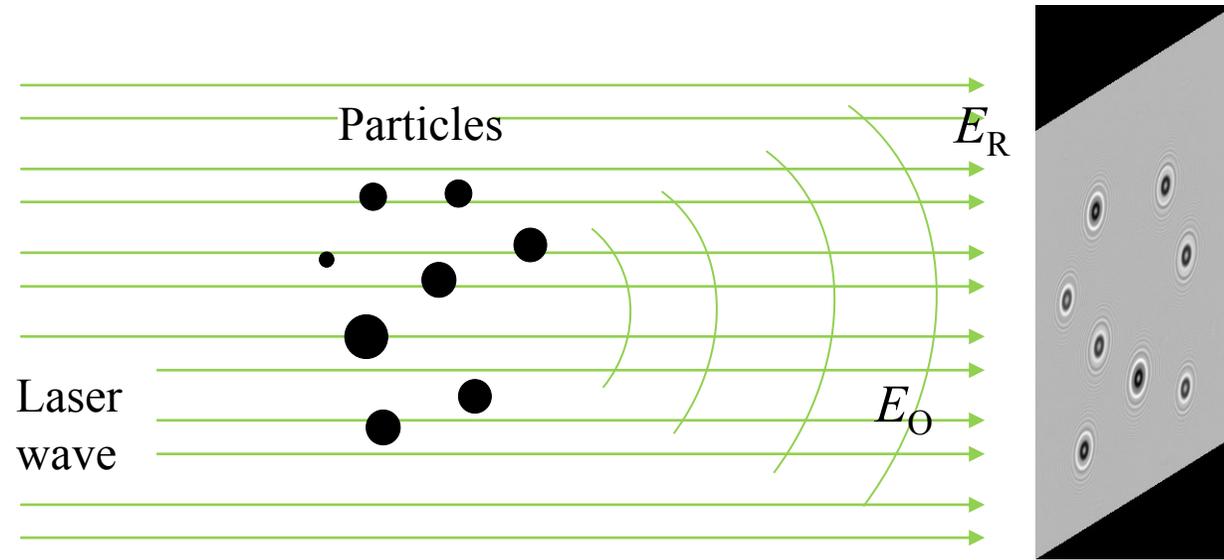
Frame rate: 20 kHz

Ethanol drop, $\sigma = 0.0244\text{N/m}$,

$\rho_a = 1.177\text{kg/m}^3$, $d_0 = 2.34 \pm 0.02\text{mm}$

$We = 11$, bag breakup, $We = 25$ for multi-mode breakup in experiments

Method: Digital in-line holography (DIH)



Recording

$$I_H = |E_O + E_R|^2 = I_O + I_R + E_O E_R^* + E_O^* E_R$$

E_O is object wave that is scattered by particles (at the recording plane)

$E_R = 1$ is undisturbed reference wave

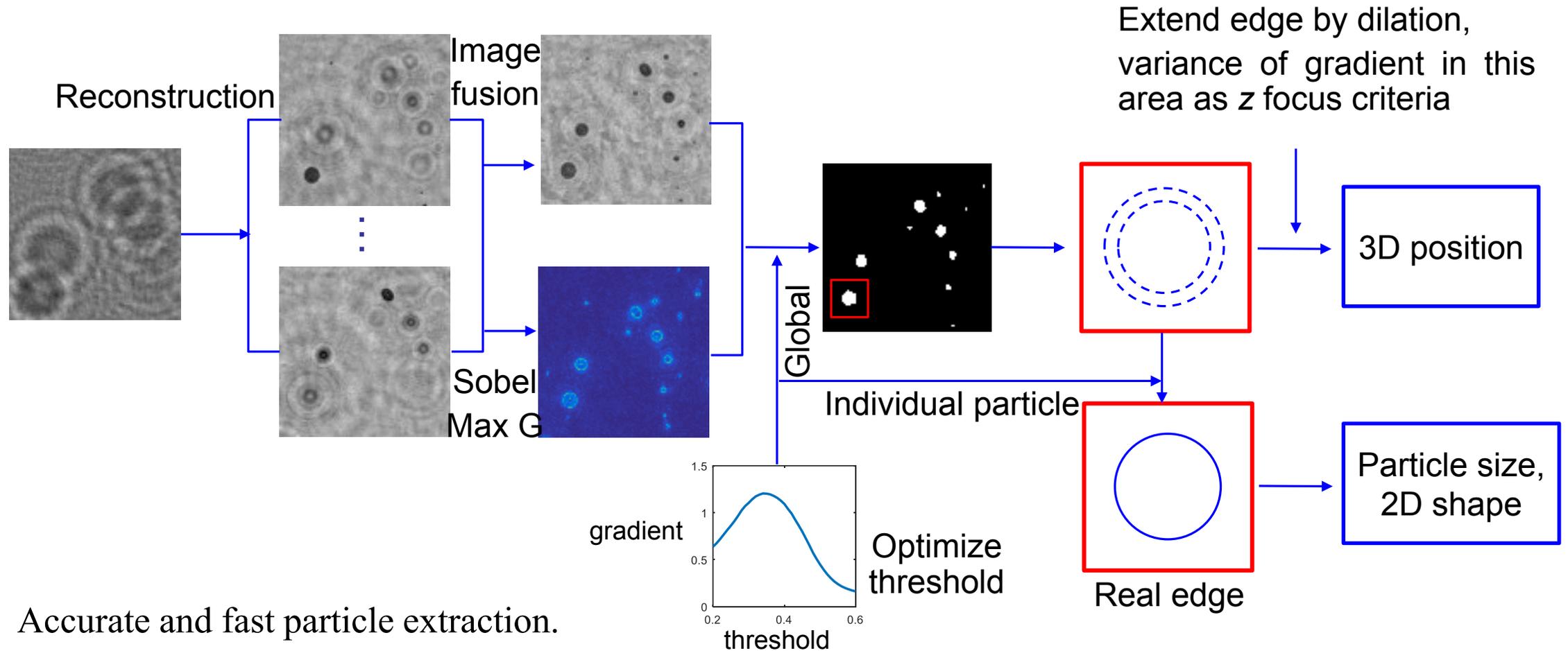
Reconstruction

$$E_R^* I_H = \underbrace{E_R^* I_O + E_R^* I_R}_{\text{DC term}} + \underbrace{E_O E_R^* E_R^*}_{\text{virtual image}} + \underbrace{E_O^* I_R}_{\text{real image}}$$



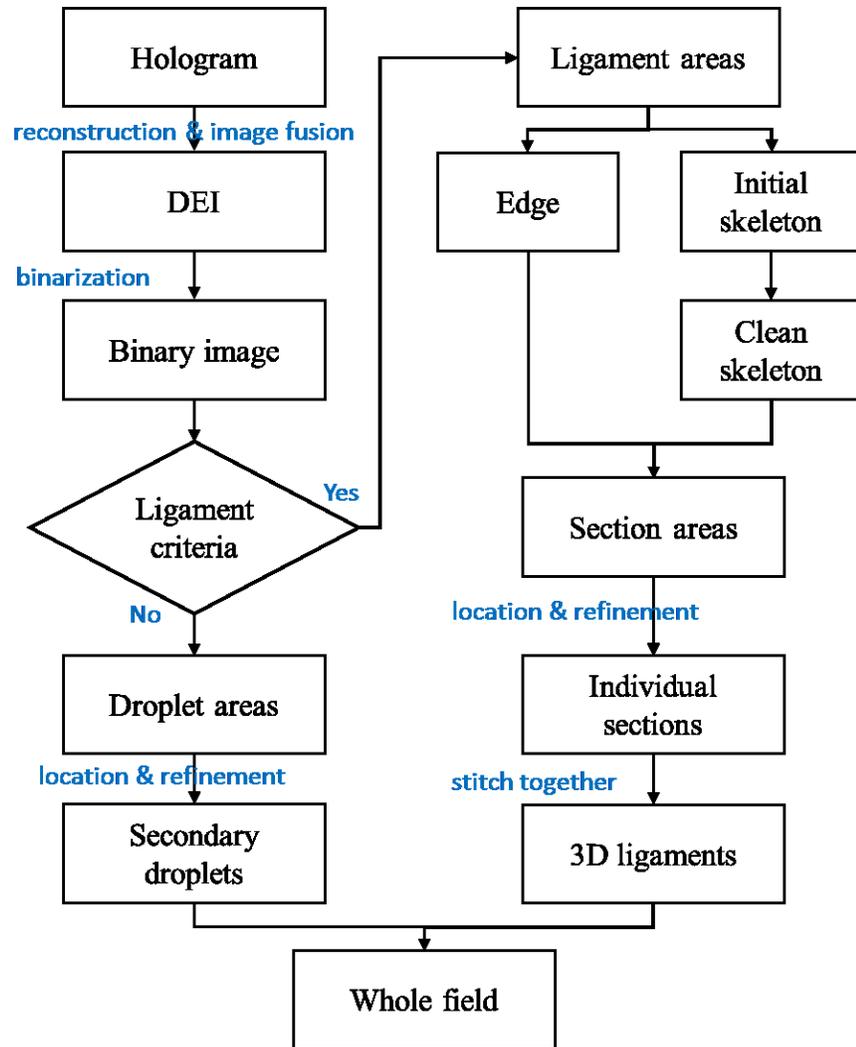
Back propagation along depth position (z)

Method: Particle extraction

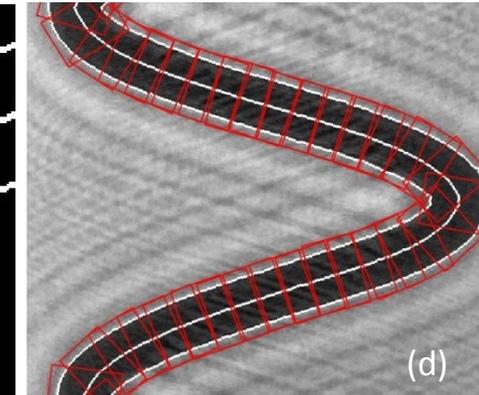
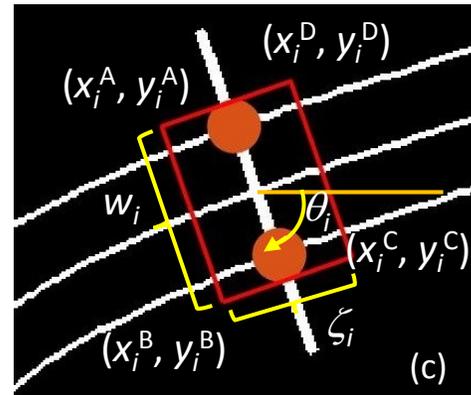
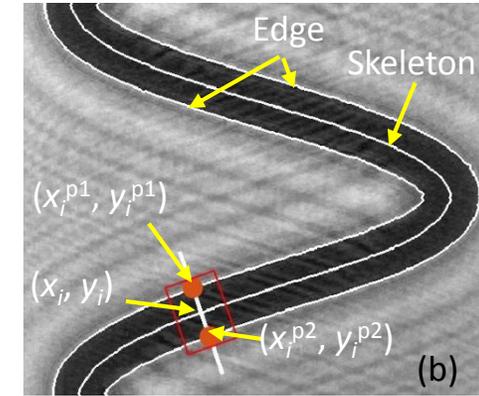
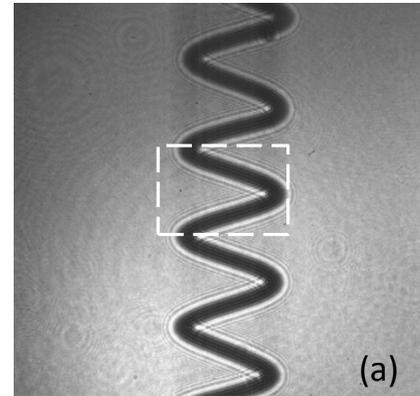


- Accurate and fast particle extraction.
- z location is not vulnerable to edge errors.

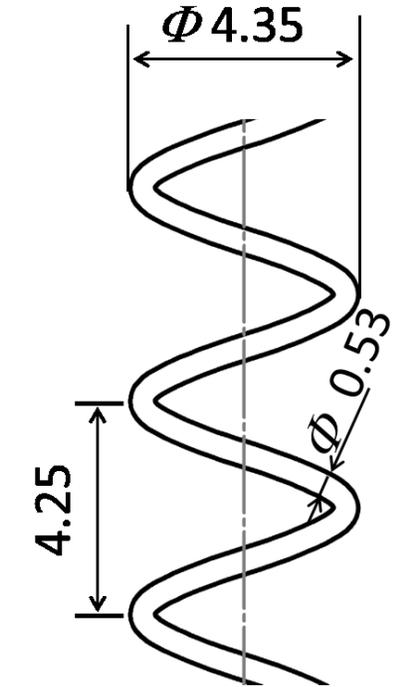
Method: Ligament extraction



Steps to extract ligaments and fragments



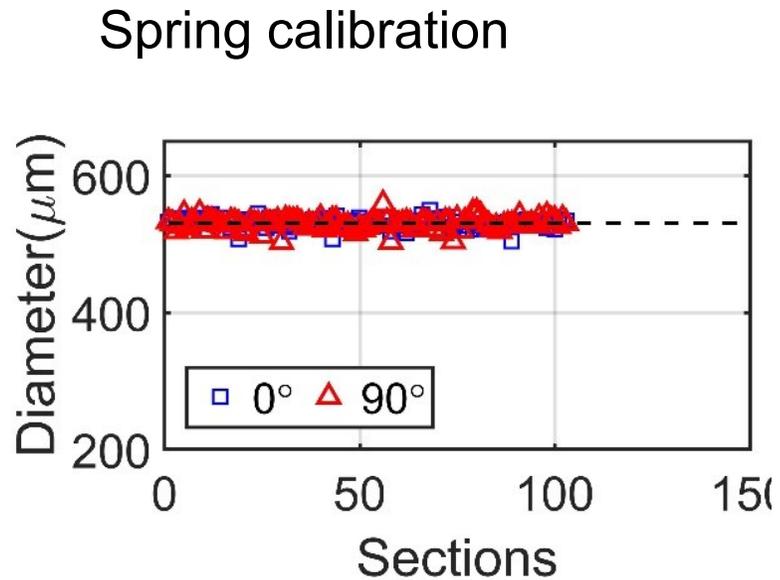
Unit: mm



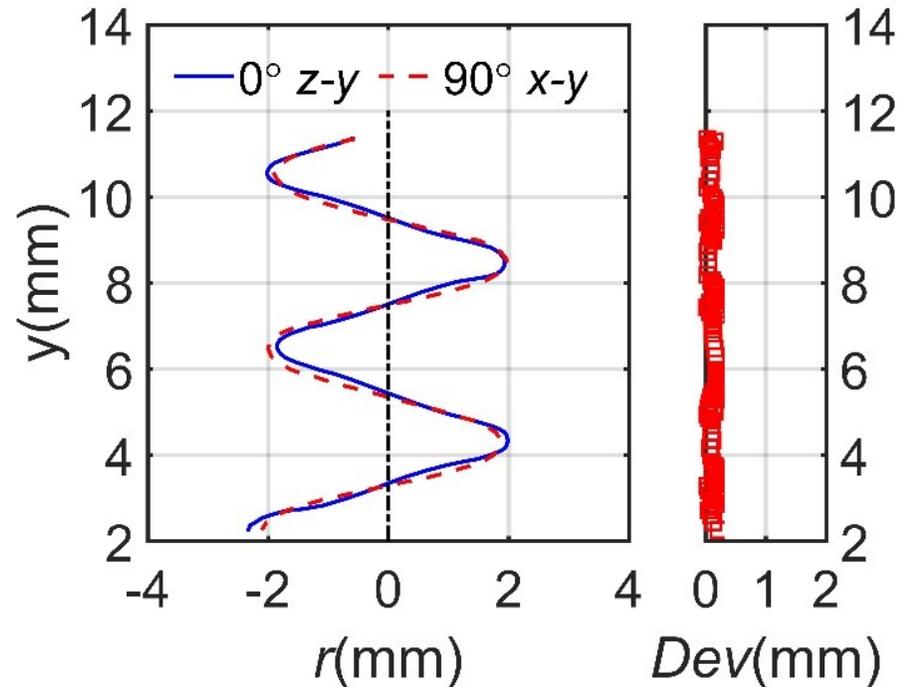
Helical spring demonstration

- Obtain edge and skeleton
- Determine local section in the red box
- Locate z position of local section as an individual particle
- Stitch local sections to be an entire ligament

Results: Calibration



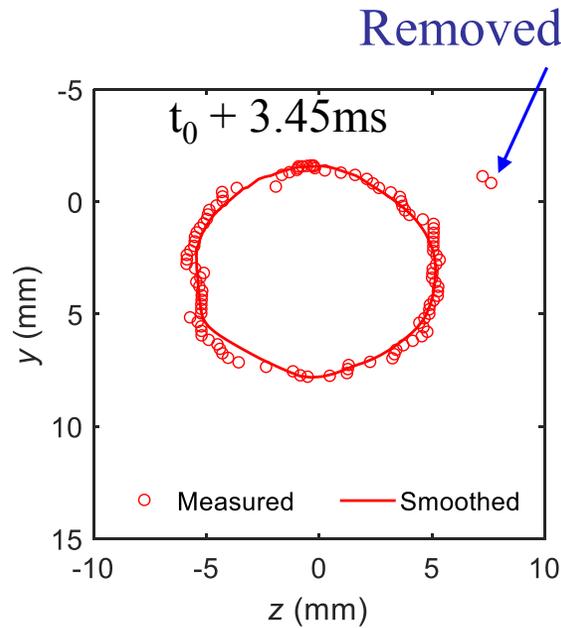
Diameter uncertainty



z position uncertainty

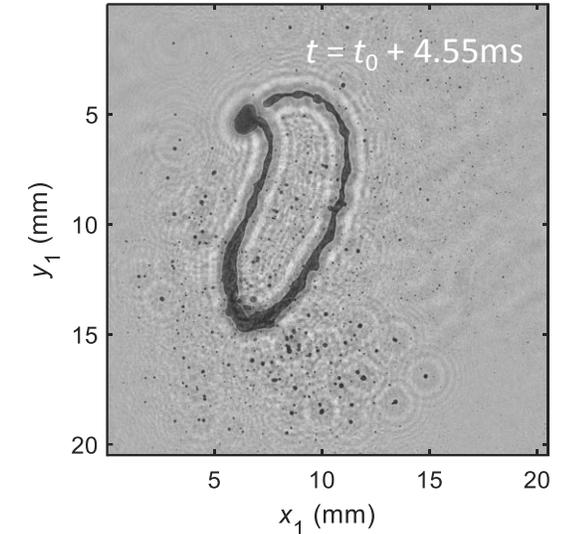
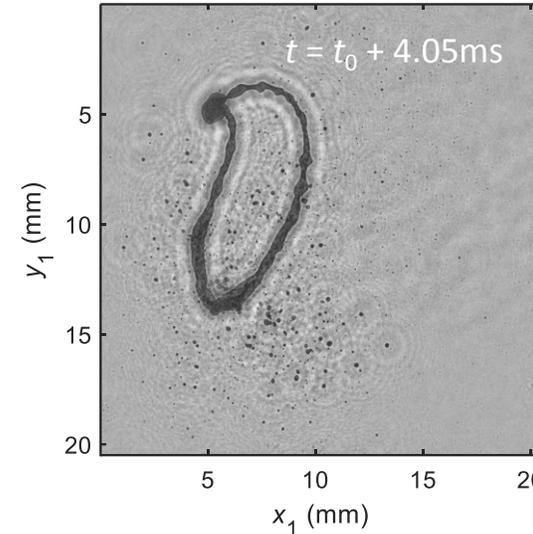
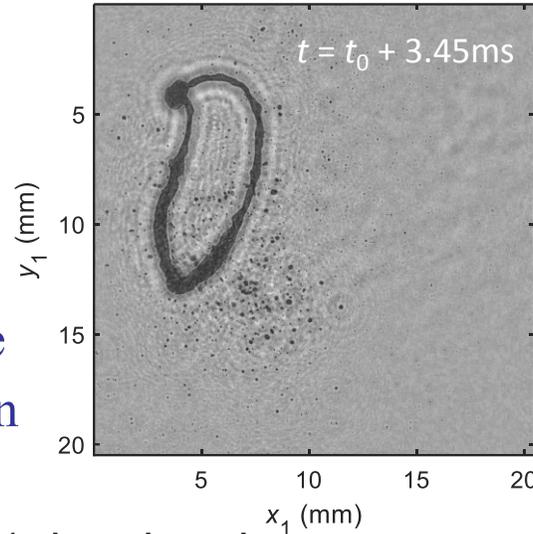
- Diameter error is about ± 1 pixel
- Raw z location error is about ± 10 pixel
- Robust local linear regression is applied to smooth the z position and remove outlier.

Results: Ligament extraction



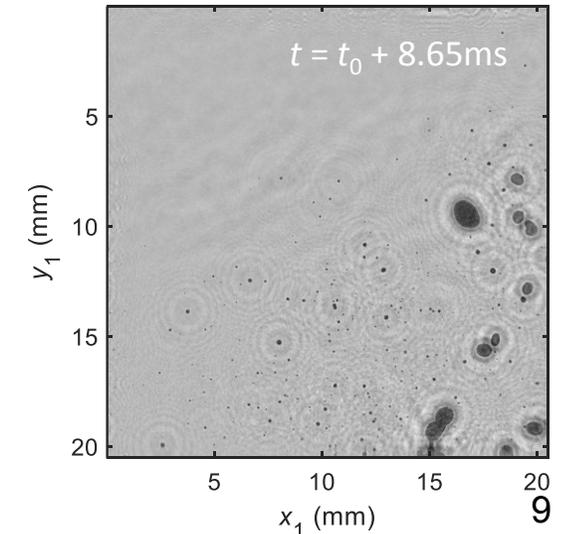
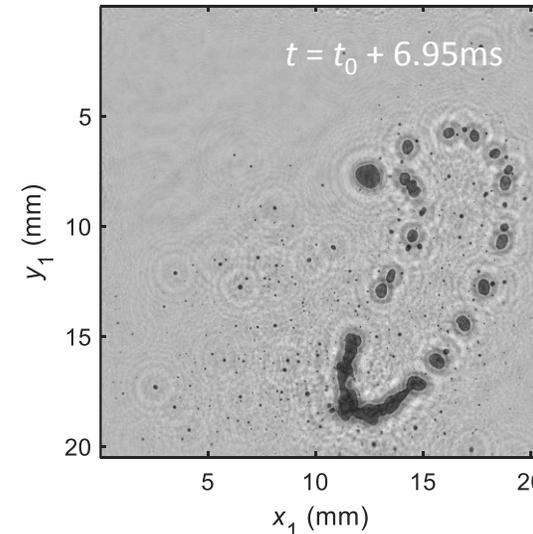
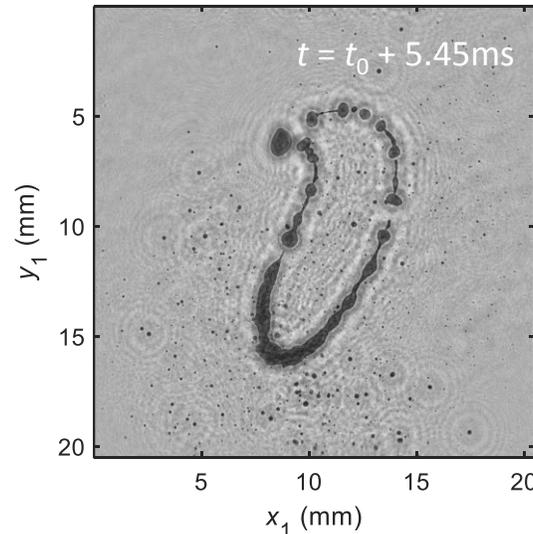
← Accurate
z location

$We = 11$, bag breakup



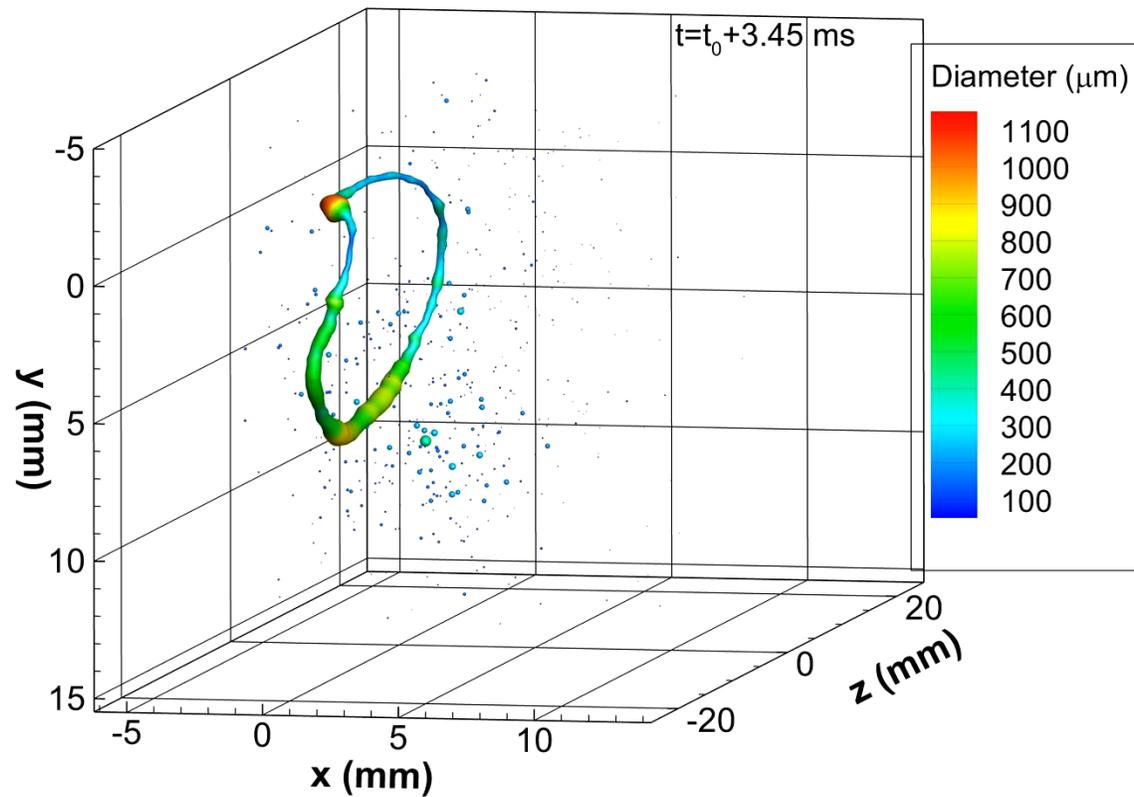
Depth-of-field extended images

- Optimal threshold ensures accurate size
- z smoothness improves local z position accuracy
- Ligament evolution are obtained from sequential holograms

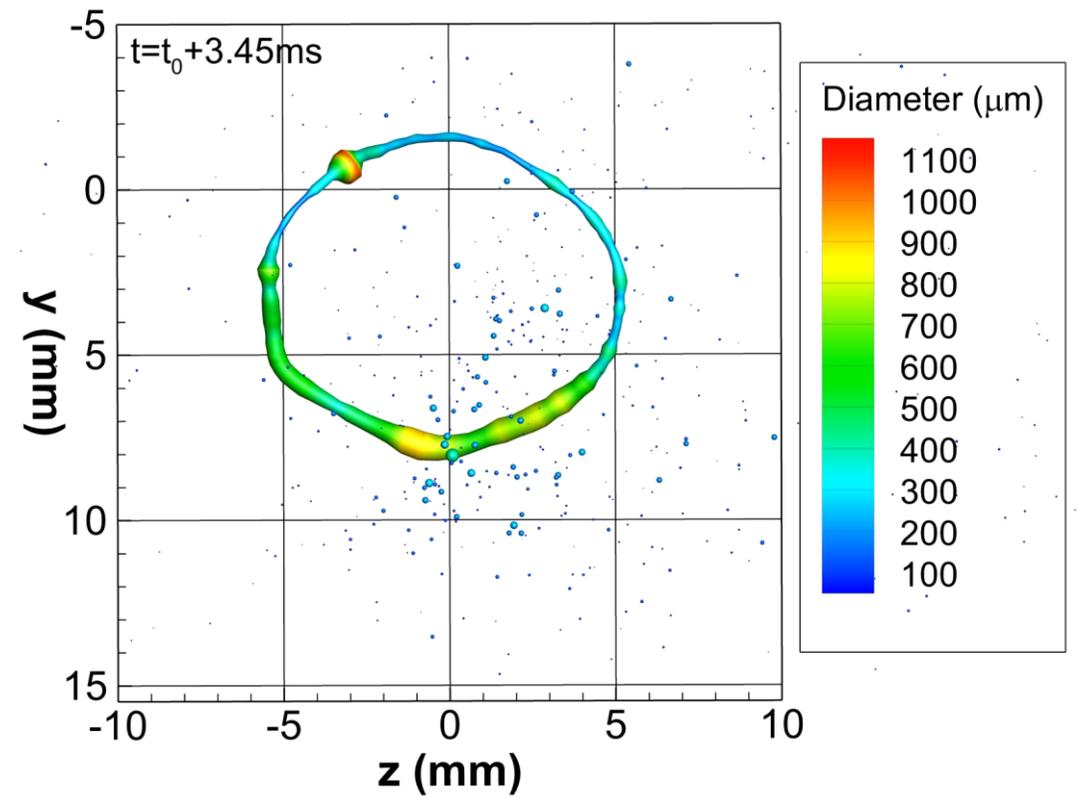


Results: Ligament evolution

Rim/ligaments are reconstructed and 3D visualized during 5ms after bag burst (15 selected frames)

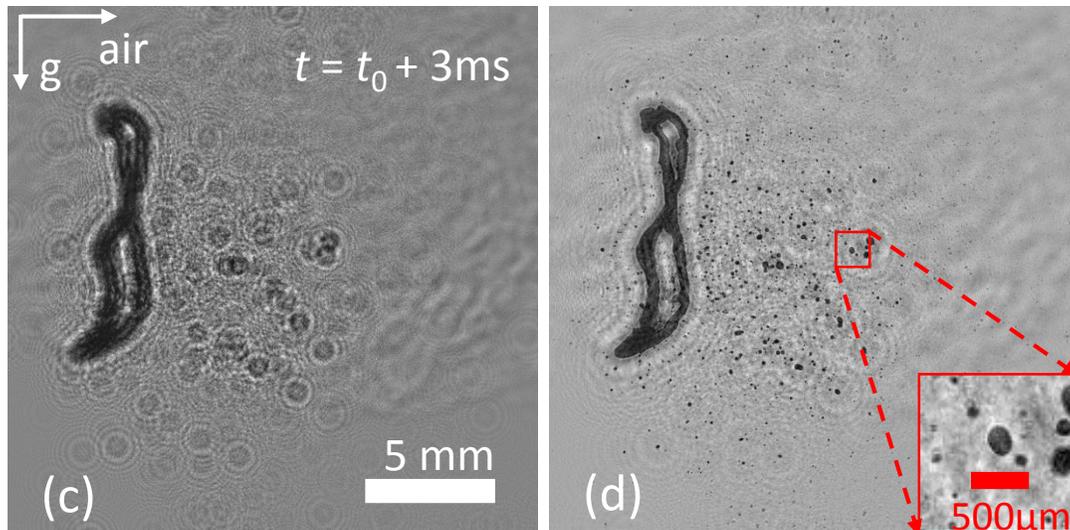
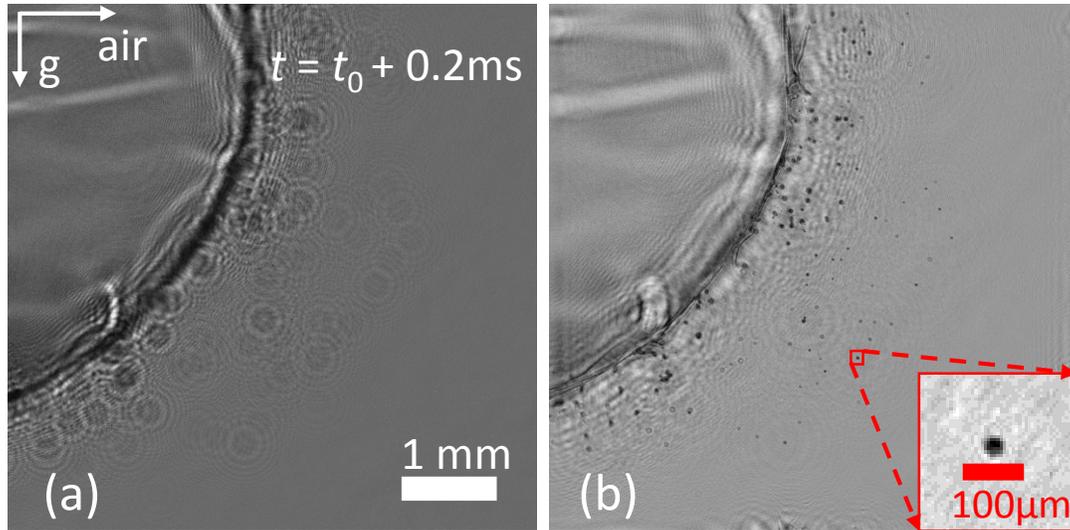


3D view (video)



z - y view (video)

Results: Fragment extraction



A magnifying lens is used for droplets at bag burst

Bag burst:

- Small droplets ($< 30\mu\text{m}$)
- 3.64X (5.5 μm pixel size)
- Within $\sim 0.5\text{ms}$ after tip burst.
- Higher velocity (up to 9m/s)

Bag fragmentation:

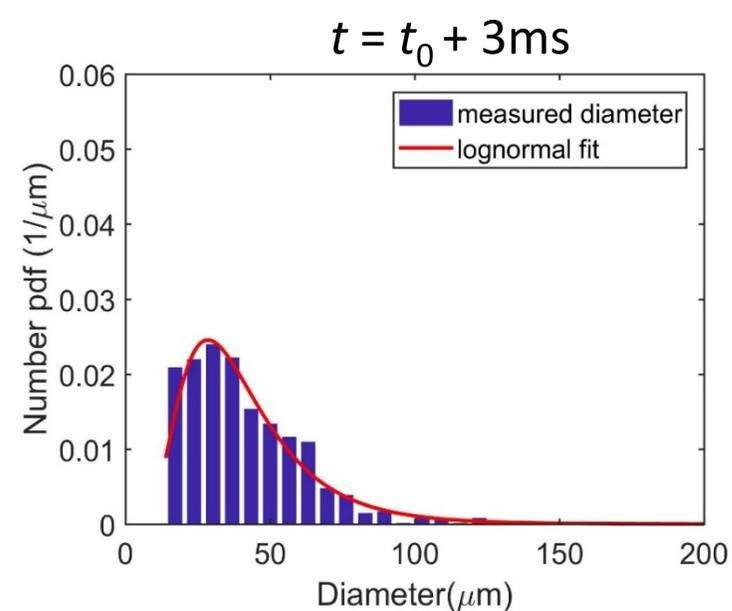
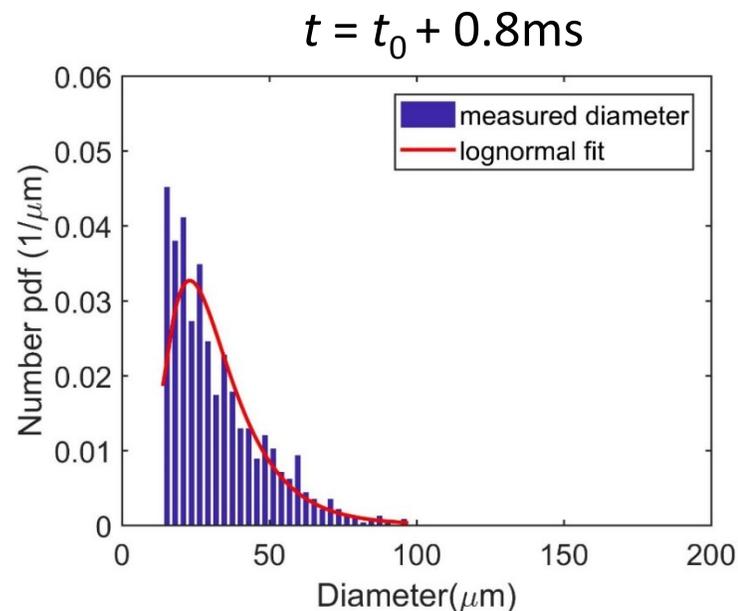
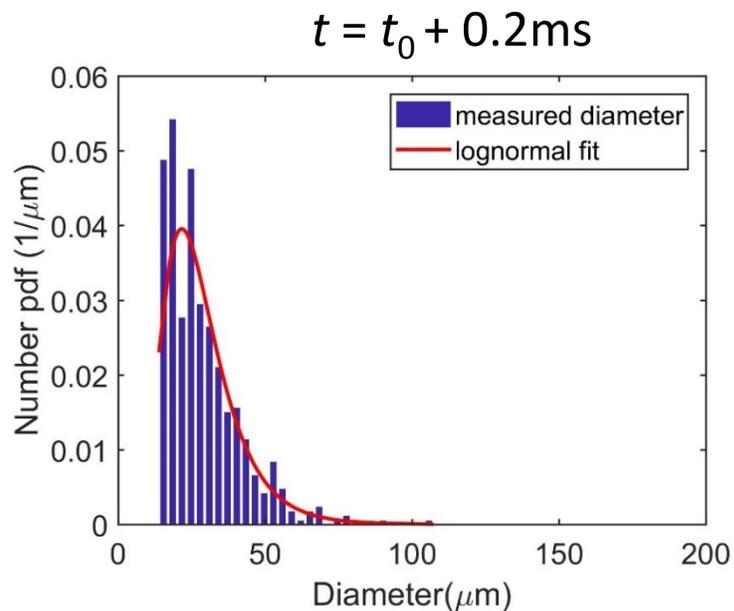
- Larger droplets (50-300 μm)
- 1X (20 μm pixel size)
- 0.5-4ms after tip burst.
- Lower velocity ($< 5\text{m/s}$)

Rim breakup:

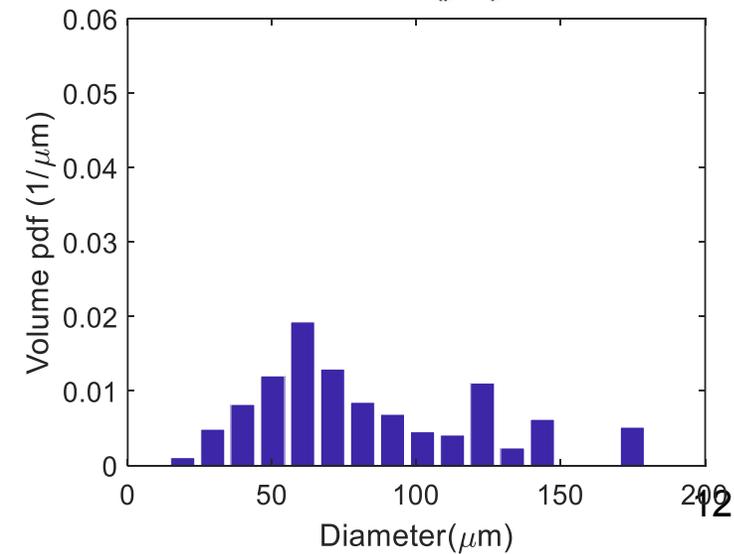
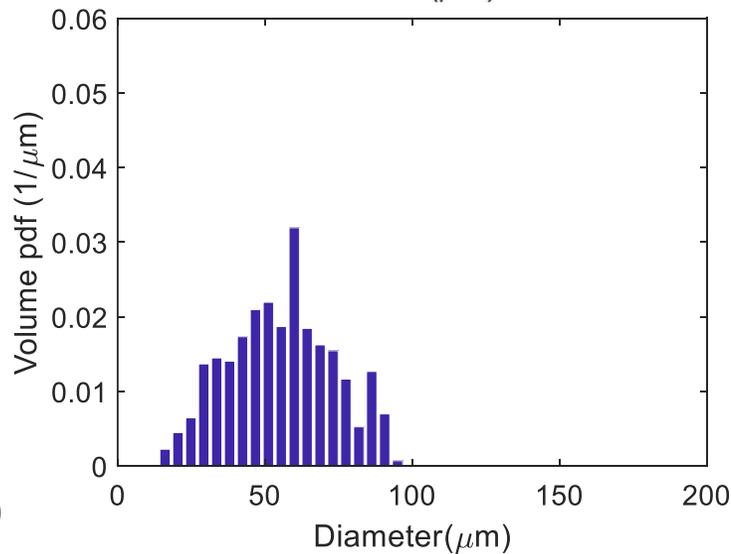
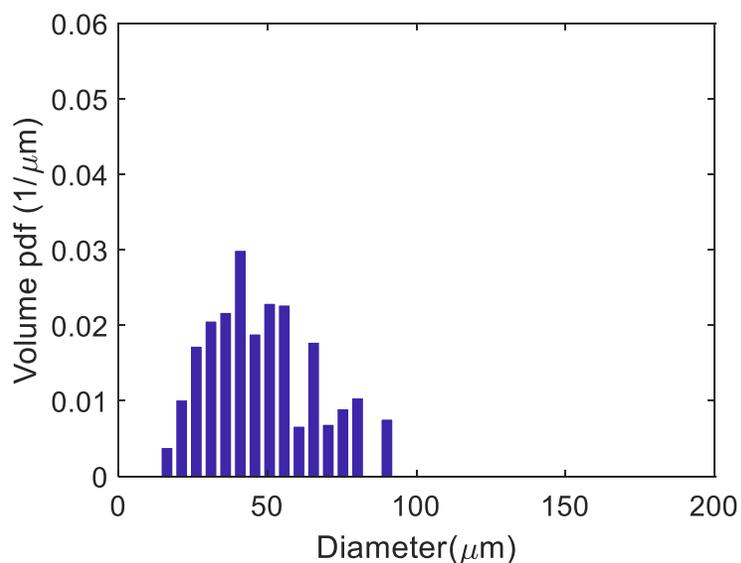
- Even larger droplets (may be $> 500\mu\text{m}$)
- Not detailed in our study

Results: Fragment size

Number
PDFs

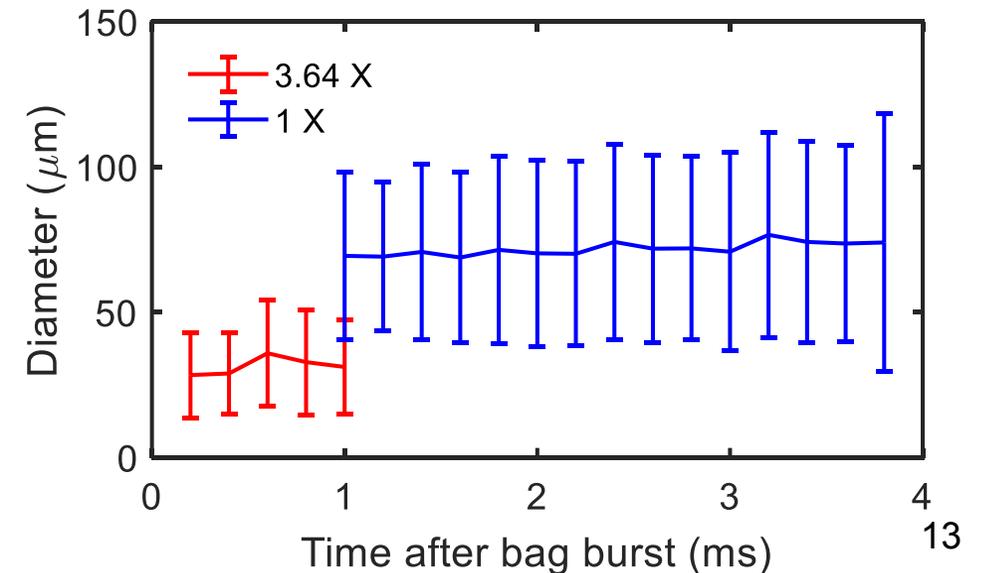
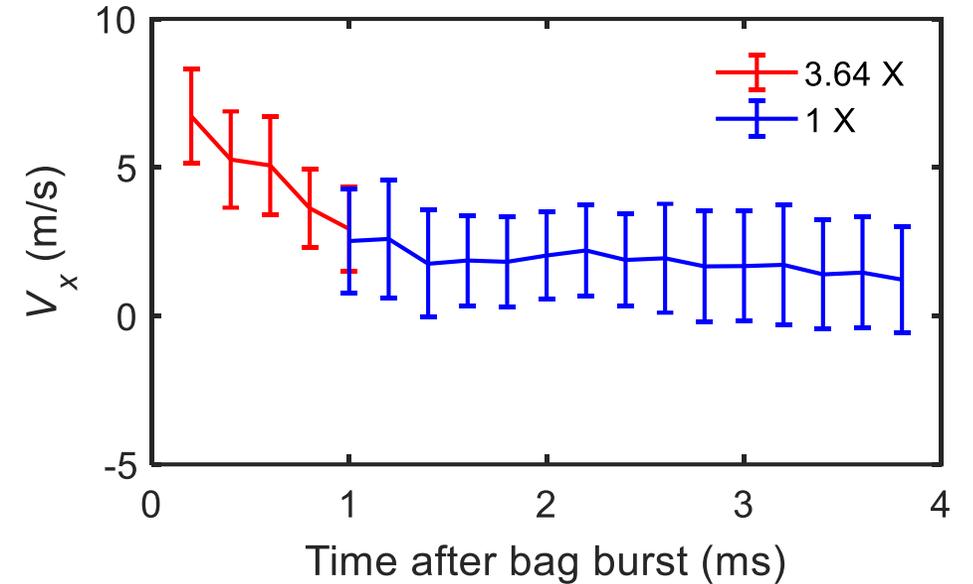
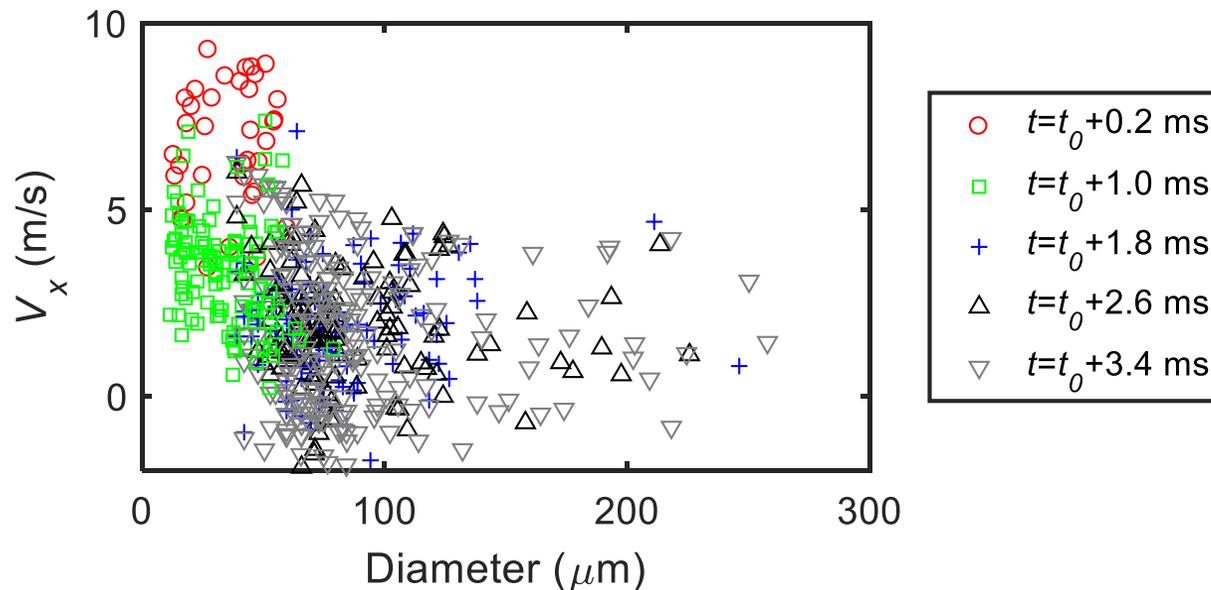


Volume
PDFs

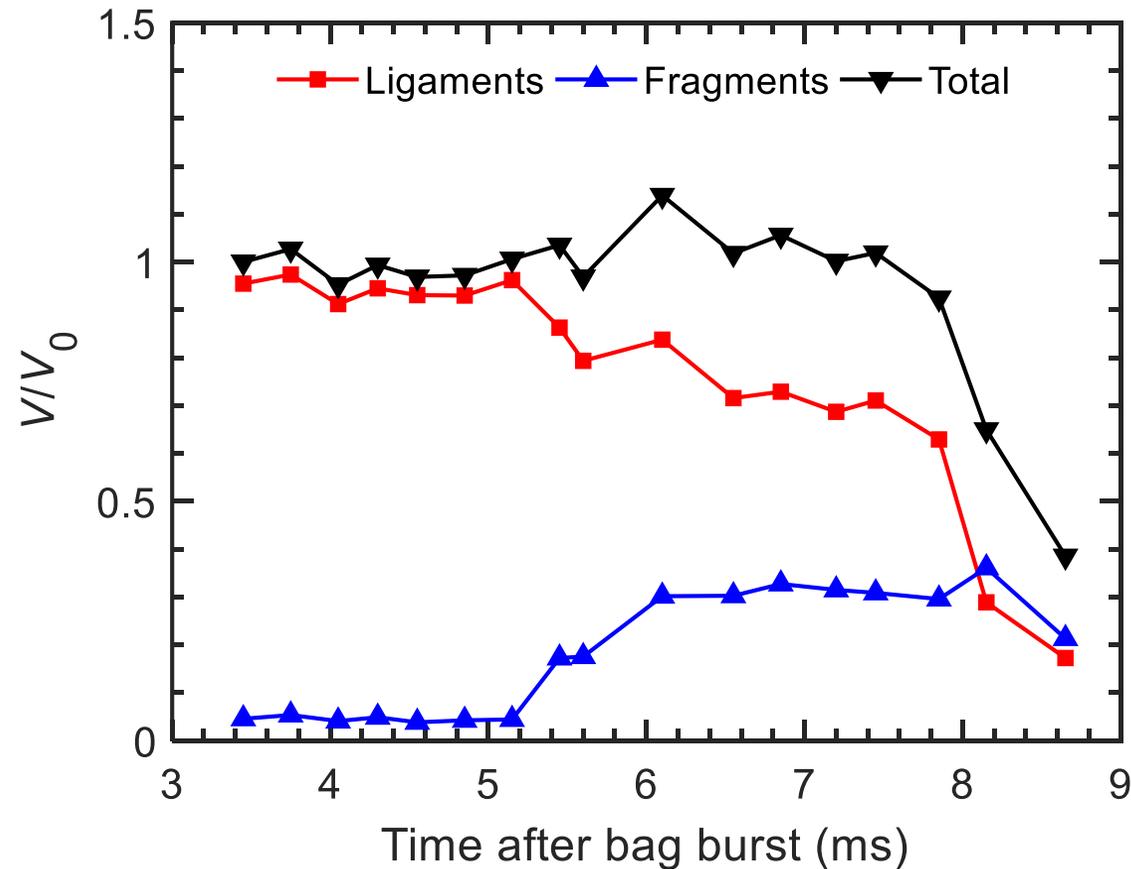


Results: Fragment evolution

- Droplets move faster at bag burst, slower at bag fragmentation. Even negative velocities appear because of back propagation of the bag wall.
- Velocity shows strong relevance to time and weak relevance to diameter. The time span is too short for droplet acceleration with drag force. Initial velocity plays a more important role.
- Higher magnification is able to detect more smaller droplets but include less larger droplets. Lower magnification exclude droplets smaller than 50 μm . Thus there is a diameter gap.

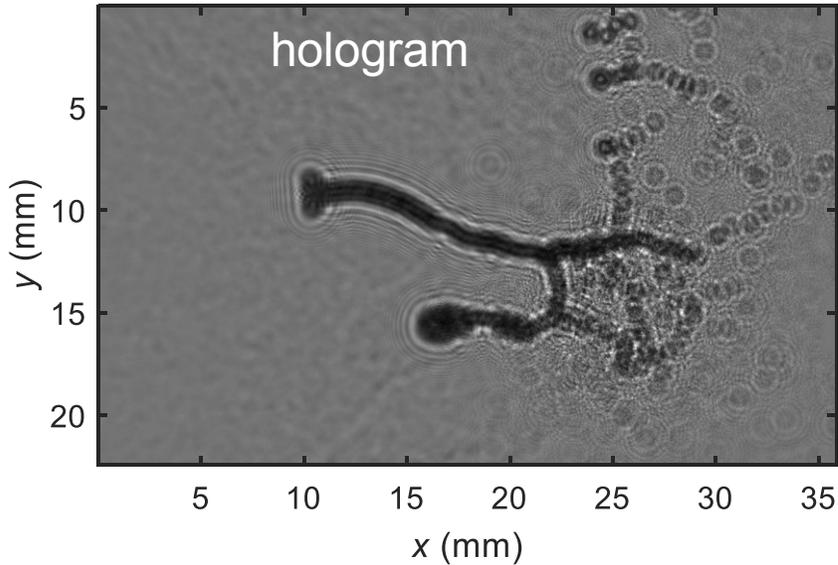


Results: Ligament-fragment volume



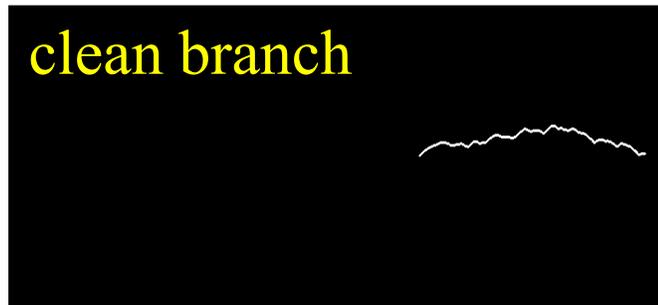
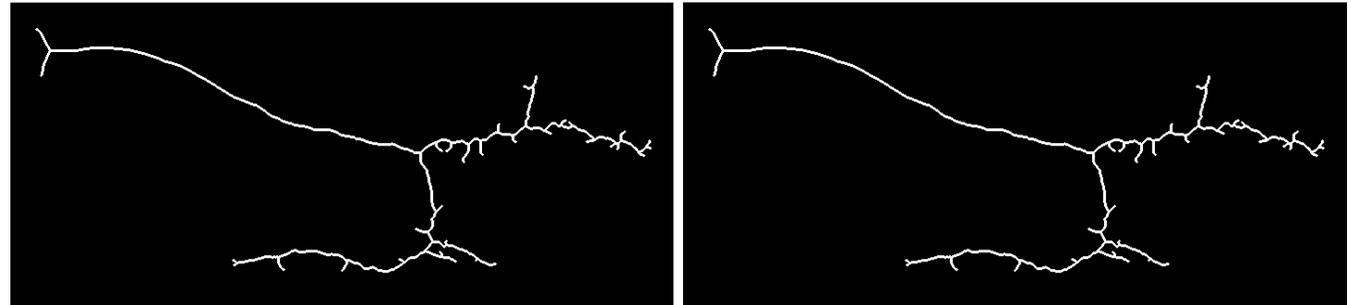
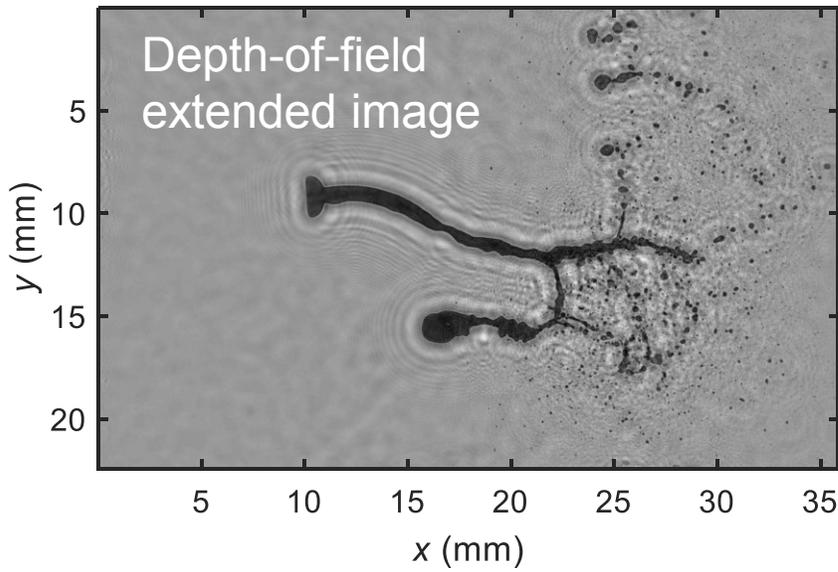
- Ligament and fragment volume is relatively stable before rim breakup.
- Rim/ligament volume transfers to fragments after rim breakup.
- Total volume of about the initial volume despite fluctuation caused by uncertainty

Results: Multi-branch ligaments



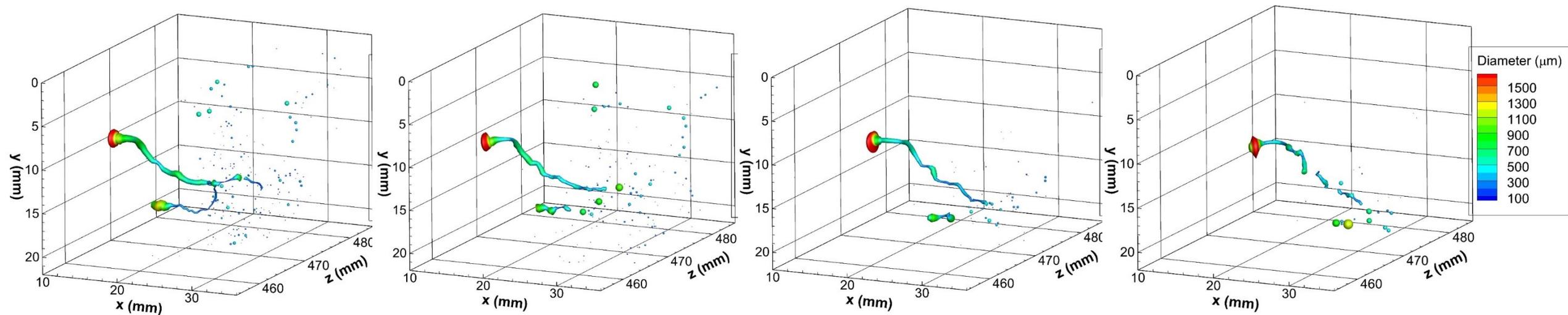
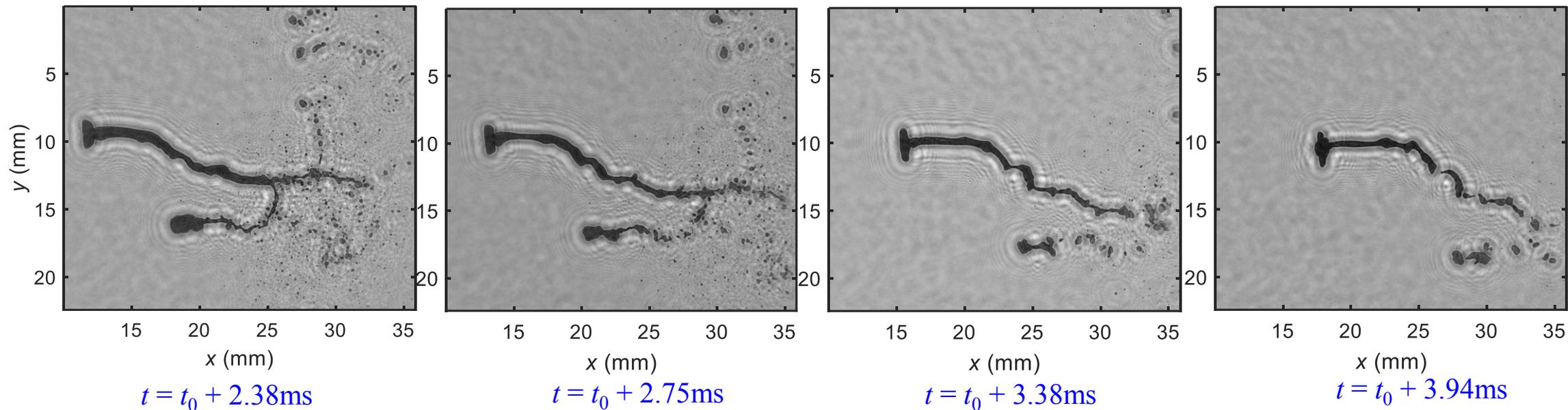
$We = 25$,
Multi-mode
breakup

- Ligament criteria: Major axis length $> 2\text{mm}$, aspect ratio > 5 or solidity < 0.5
- Remove the spurs
- Separate branches and save them
- Deal with each branch and stitch them together



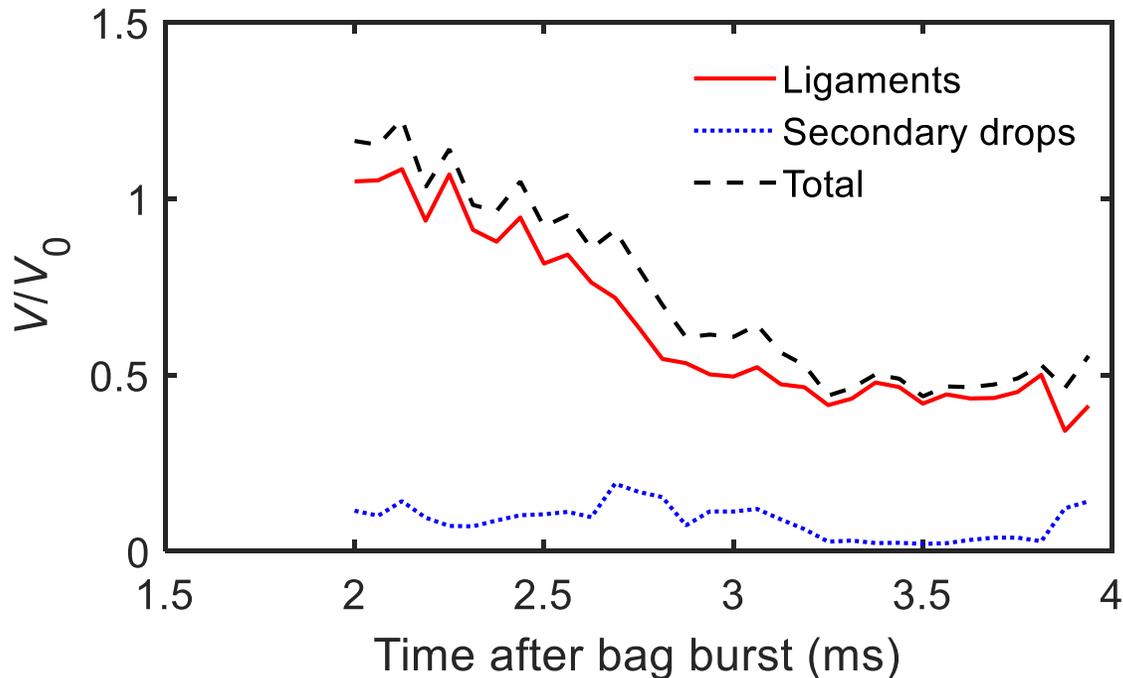
Measurement of multi-branch ligament is an improvement.

Results: Multi-branch ligaments



Results: Multi-branch ligaments

Volume evolution is studied from 32 frames during 1.94ms



Relatively large uncertainty (up to 17%) is probably due to

- Bag residues may be recognized as compact ligament
- Overlap problem
- 5% size error will lead to ~14.5% volume error

Conclusions

1. 3D morphology and evolution of rims and ligaments in bag and multi-mode breakup is measured using an automatic algorithm.
2. With a small tilted angle, overlap problem is to some extent avoided.
3. Time-resolved size and velocity of fragments are analyzed by using two magnification for different stages.
4. Volumes of rim/ligament and secondary droplets add up to nearly 100%, despite some fluctuation caused by measurement uncertainty.
5. Analytical work is expected to explain the interesting results (e.g. multi-modal size distribution and back-propagation of fragments) in the future.

Thank You for Your Attention!