



Stochastic modeling of primary atomization : application to Diesel spray.

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Introduction.



Sacadura ,CORIA

Atomization: main phenomena:

Turbulence in liquid and gaz phase,
cavitation, cycle by cycle variations

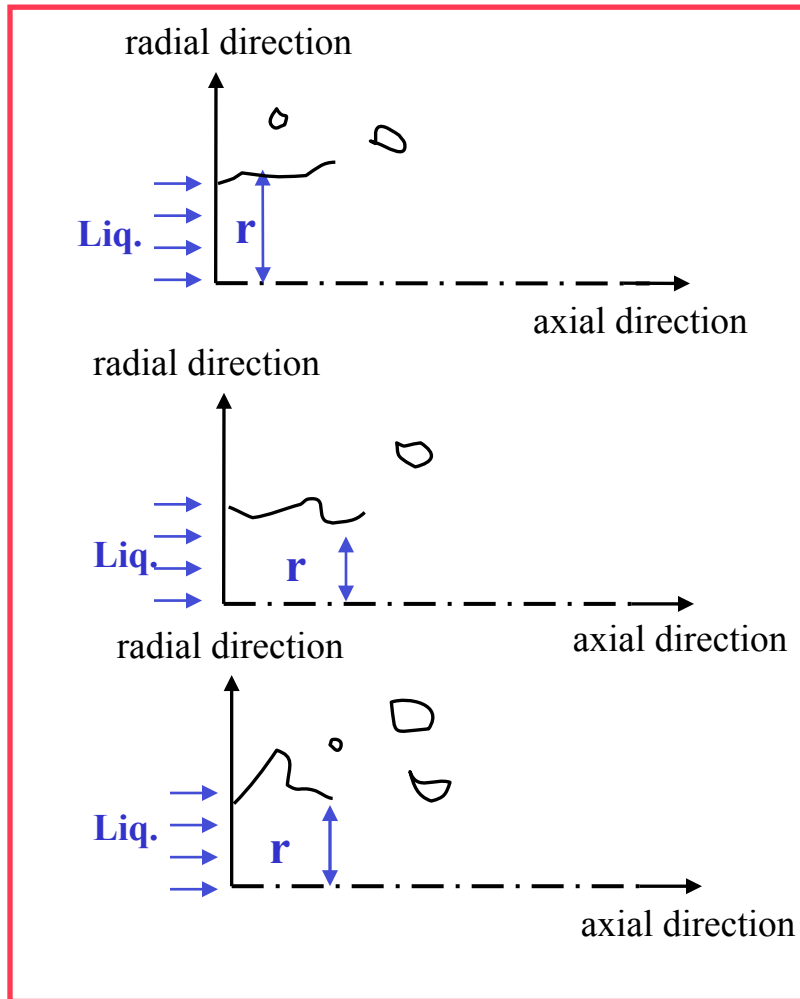
⇒ Deterministic description of such
atomization is very difficult task.

⇒ Stochastic approach

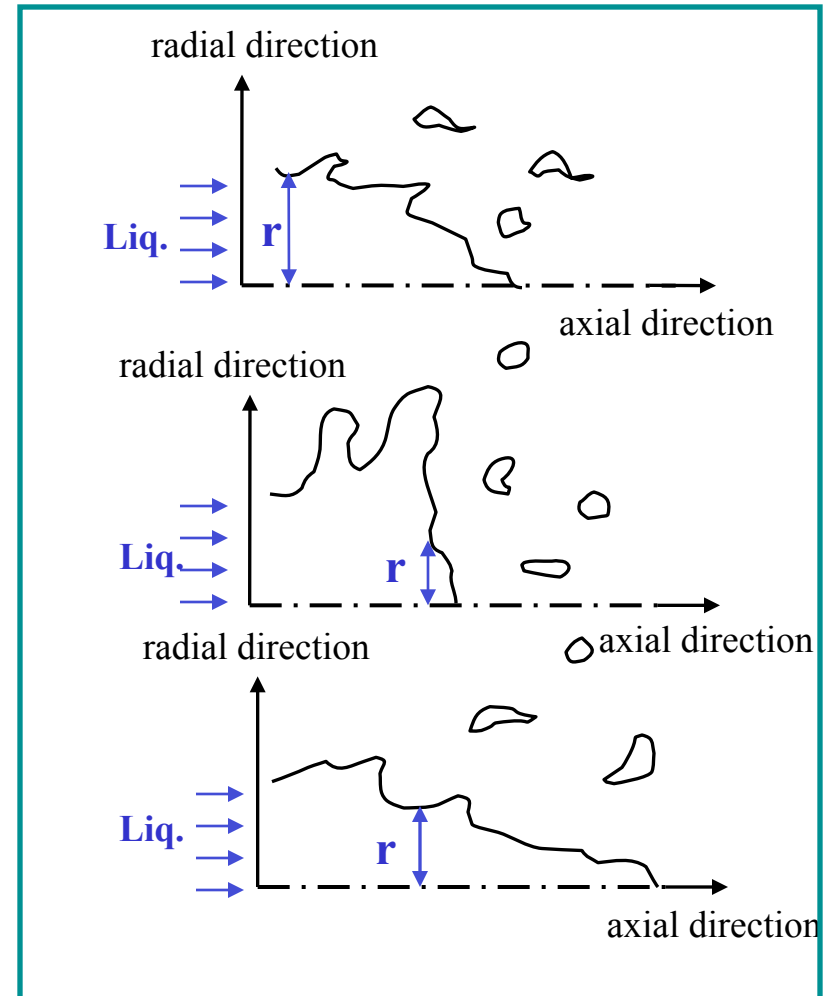
⇒ Application to primary atomization.

Floating cutter particles.

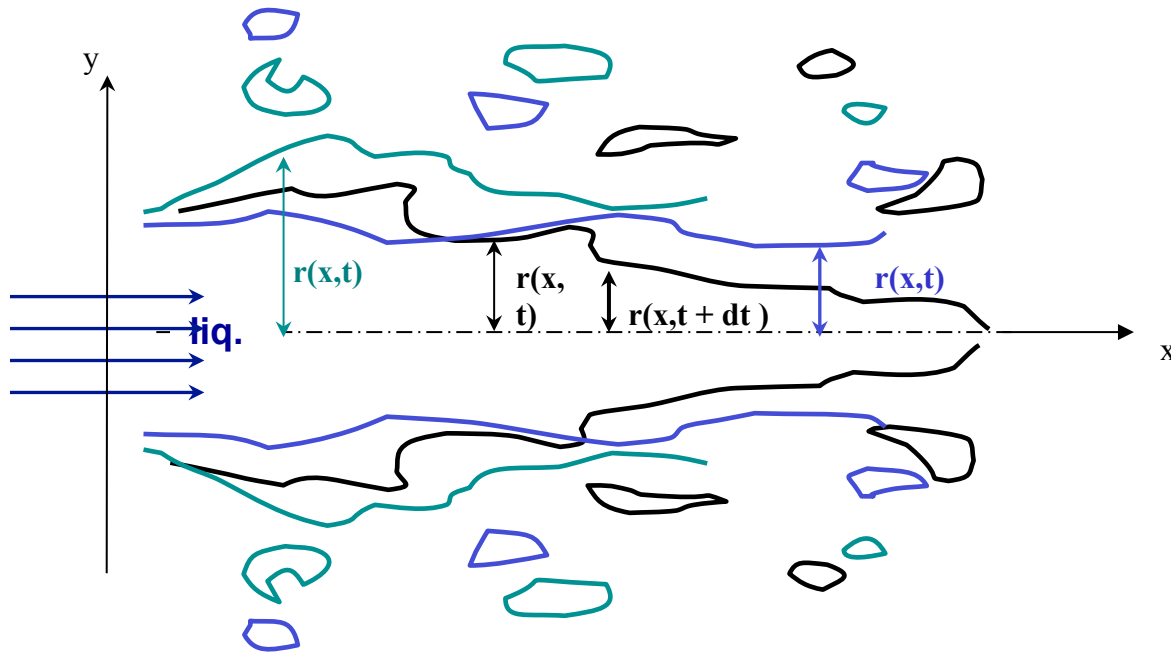
Time t1



Time t2



The main assumption: scaling symmetry for thickness.



1. Scaling symmetry for thickness of liquid core.

$$r(x,t+dt) = \alpha r(x,t)$$

$$0 < \alpha < 1$$

$$\downarrow$$
$$q(\alpha)$$

**Fragmentation
intensity spectrum**

2. Life time.
3. Ensemble of n particles.

Theory of Fragmentation under Scaling symmetry (Gorokhovski & Saveliev 2003, Phys. Fluids).

Evolution equation

$$\frac{\partial f(r,t)}{\partial t} = \nu \int_0^1 f\left(\frac{r}{\alpha}, t\right) q(\alpha) \frac{d\alpha}{\alpha} - \nu f(r,t) \longrightarrow \text{Knowledge of } q(\alpha)$$

Fokker Planck type equation

$$\frac{1}{\nu} \frac{\partial f(r,t)}{\partial t} = -\langle \ln \alpha \rangle \frac{\partial}{\partial r} (r f(r,t)) + \frac{\langle \ln^2 \alpha \rangle}{2} \frac{\partial}{\partial r} r \frac{\partial}{\partial r} (r f(r,t)) \longrightarrow \text{Knowledge of } \langle \ln \alpha \rangle \text{ and } \langle \ln^2 \alpha \rangle$$

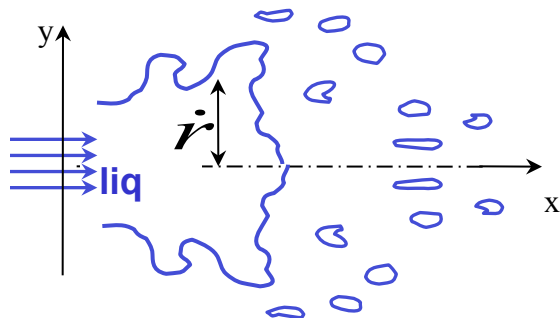
—————> Equation for the distribution function

—————> Log brownian stochastic process

Langevin type equation

—————> Equation for one realisation

$$\dot{r} = \nu \langle \ln \alpha \rangle r + \sqrt{\nu \langle \ln^2 \alpha \rangle / 2} r \Gamma(t)$$



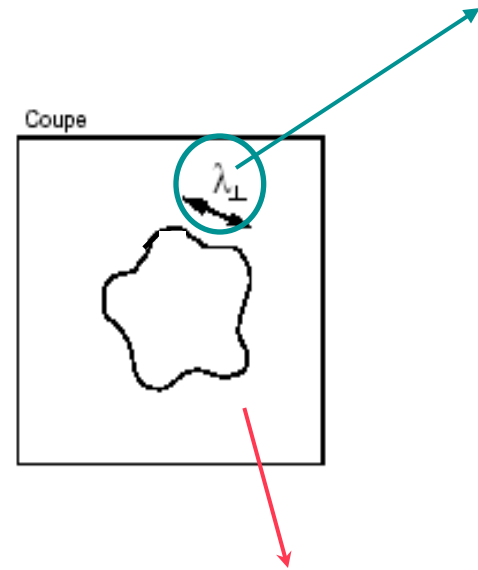
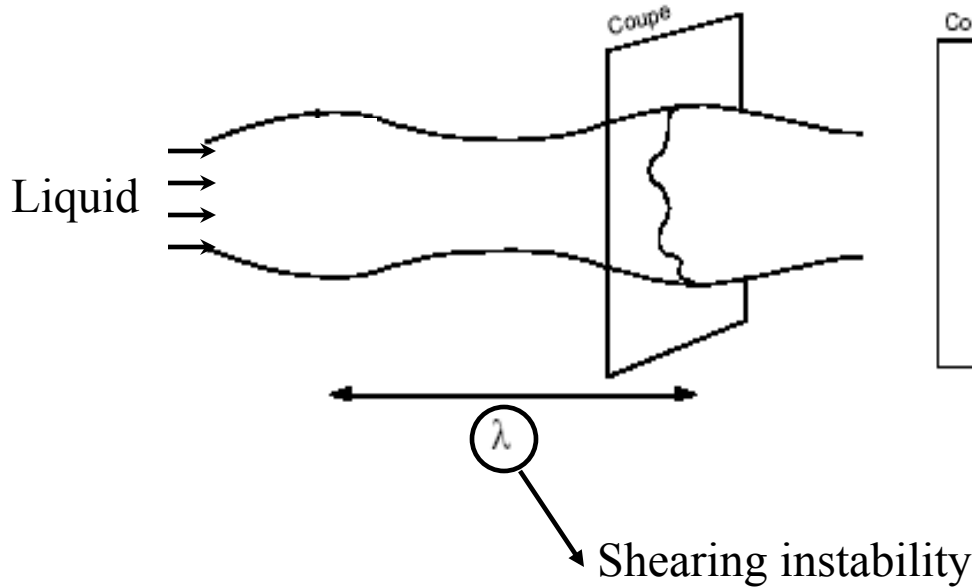
$$\frac{\langle \ln^2 \alpha \rangle}{\langle \ln \alpha \rangle} = \ln \left(\frac{r_c}{r_*} \right)$$

r_c = critical length scale

$$\langle \ln \alpha \rangle = \text{CONST} \cdot \ln \left(\frac{r_c}{r_*} \right)$$

r_* = typical length scale

Identification of main parameters.



Transverse instability

=

Rayleigh Taylor instability

Formation of droplets through a minimal size r_{cr}

$\Rightarrow r_c = \text{critical radius } r_{cr} \rightarrow We_{cr} = \frac{\rho_g (u_g - u_l)^2 r_{cr}}{\sigma}$

$r_* = \text{Rayleigh Taylor scale } \lambda_{RT}$

Time scale $\nu = \nu_{RT}$

$$\lambda_{RT} = 9.02 \frac{(1 + 9.45Z^{0.5})(1 + 0.4T^{0.7})}{(1 + 0.87We_2^{1.67})^{0.6}} r_0$$

$$\nu_{RT} = \left[\frac{\rho_l r_0^3}{\sigma} \right]^{-0.5} \frac{(0.34 + 0.38We_2^{0.5})}{(1 + Z)(1 + 1.4T^{0.6})}$$

$$We_1 = \rho_l (u_{g0} - u_{l0})^2 r_0 / \sigma$$

$$We_2 = \rho_g (u_{g0} - u_{l0})^2 r_0 / \sigma$$

$$Re_1 = (u_{g0} - u_{l0}) r_0 / \nu_l$$

$$Z = We_1^{0.5} / Re_1$$

$$T = ZWe_2^{0.5}$$

(Reitz 1987)

Realization of stochastic process; « Stochastic floating cutter particles ».

Motion of particules

In the radial direction:

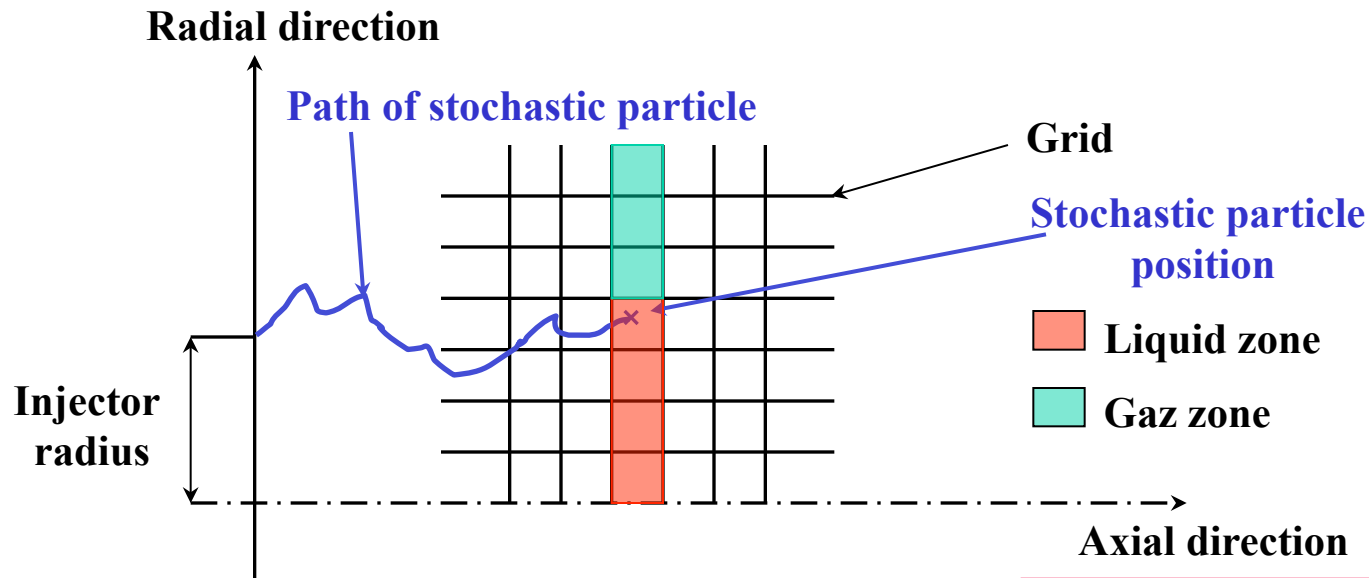
$$V_{ip} = v \langle \ln \alpha \rangle r + \sqrt{v \langle \ln^2 \alpha \rangle / 2} r \Gamma(t)$$

$$\frac{dr}{dt} = V_{ip}$$

In the axial direction:

$$\frac{dU_{ip}}{dt} = \frac{1}{2} \frac{\rho_g}{\rho_l} |u_g - u_{ip}| \frac{|u_g - u_{ip}|}{r}$$

$$\frac{dx_{ip}}{dt} = U_{ip}$$

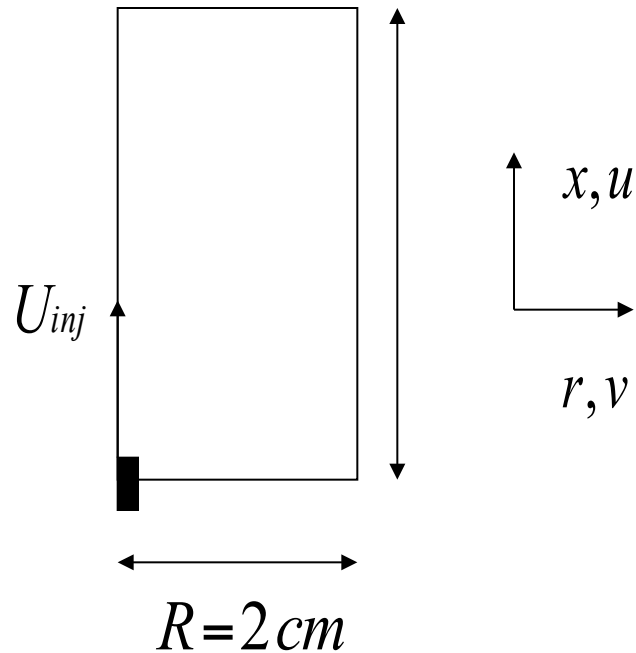


=>

Statistics of liquid core boundary

Experimental setup.

C. Arcoumanis, M. Gavaises, B. French SAE Technical Paper Series, 970799 (1997).



Gaz initial conditions:

Atmospheric conditions

$$T = 300^\circ K$$

$$p = 1\text{ bar}$$

Liquid initial conditions:

$$\rho_p = 0.8\text{ g / cm}^3$$

$$R_{inj} = 0.009\text{ cm}$$

$$t_{inj} = 0.85\text{ ms}$$

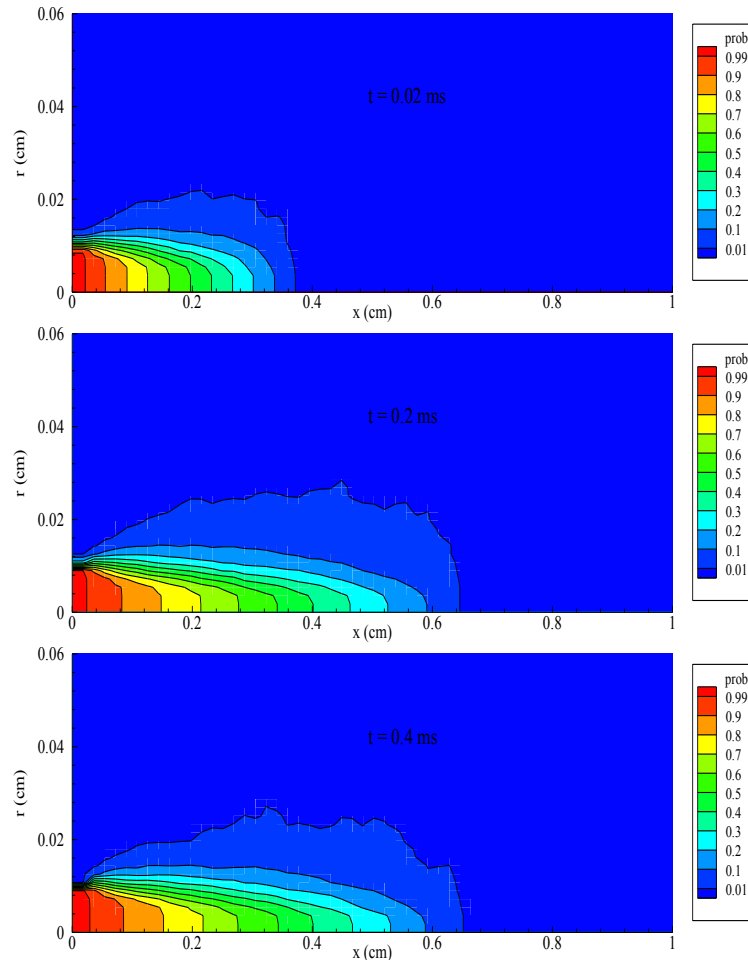
$$m_{inj} = 3.2\text{ mg}$$

$$T_{inj} = 300^\circ K$$

$$U_{inj} = U_{inj}(t) = 0 \div 260\text{ m/s}$$

Probability to get liquid core; formation of discret blobs using presumed distribution:

Statistics of liquid core boundary



Injection of droplets

Radius:

$$f(r) = \frac{1}{r_{typ}} \exp\left(-\frac{r}{r_{typ}}\right)$$

$r_{typ} \rightarrow$ Radius of the injector

Mass flow rate conservation

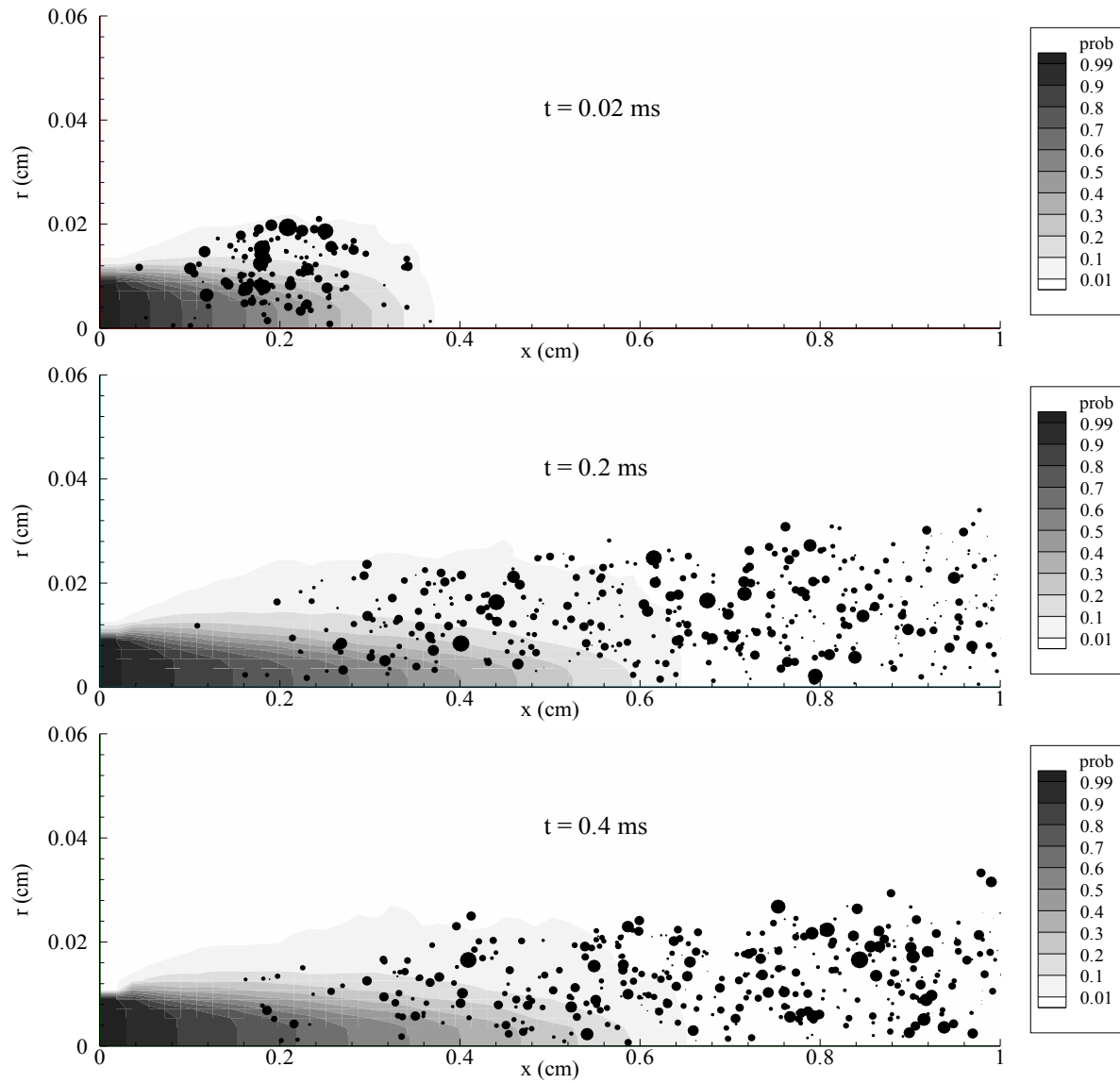
Motion of droplets

\Rightarrow Standard KIVA procedure with velocity conditioned on the presence of liquid

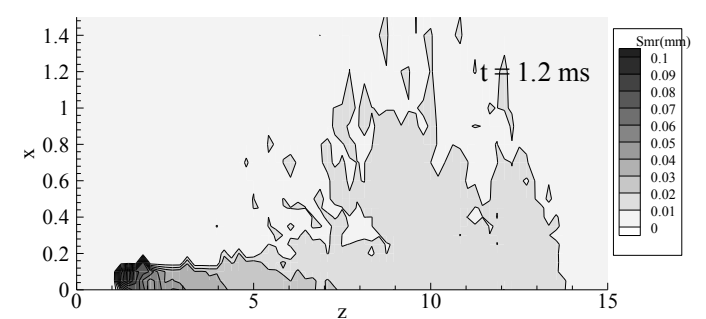
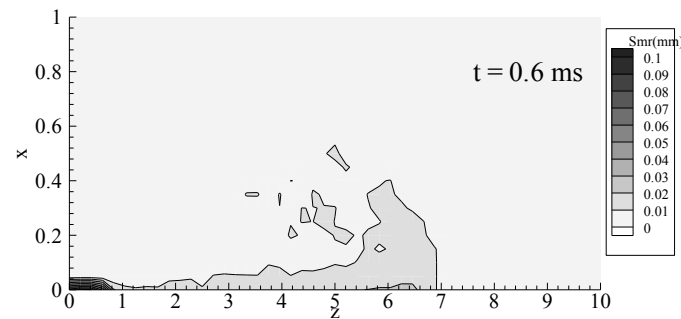
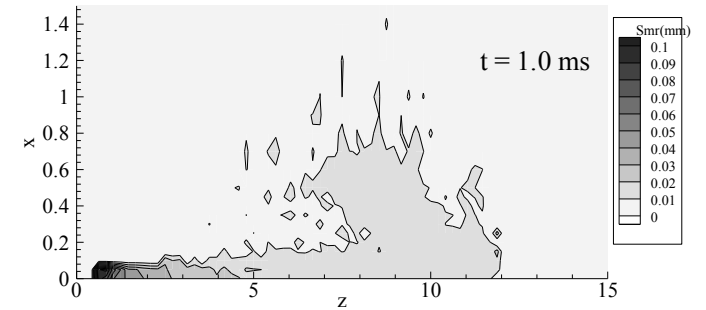
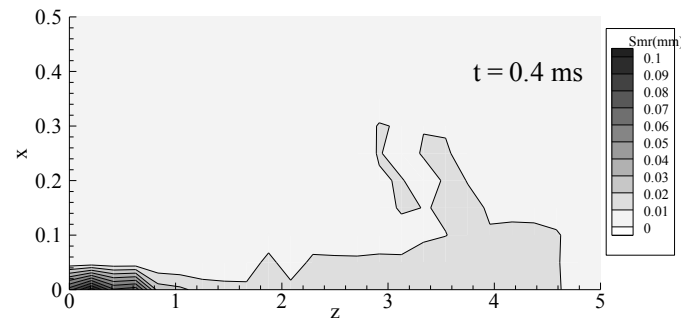
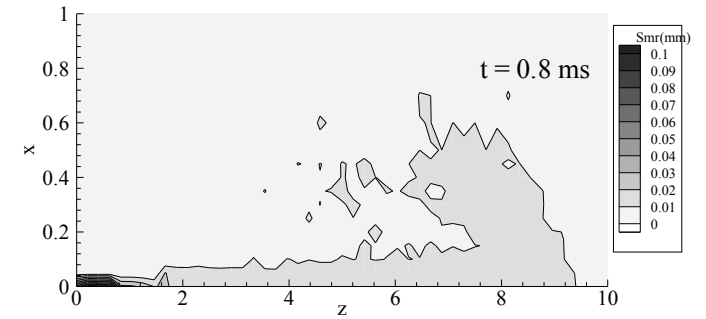
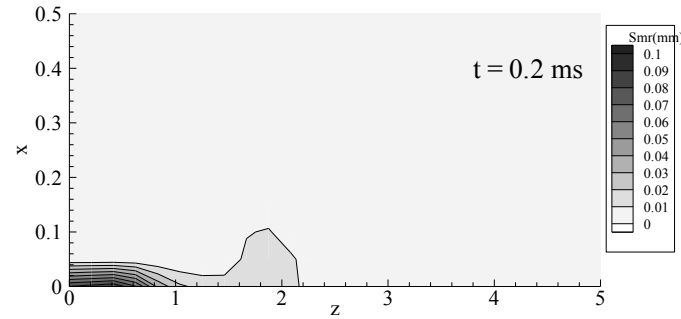
Initial conditions \rightarrow Injection velocity $u_p = U_{inj}(t)$

\rightarrow $v_p = \frac{rad_p}{\tau} = \sqrt{K_{liquid}} \sqrt{\frac{\rho_g}{\rho_p}}$

Example of distribution of formed blobs.



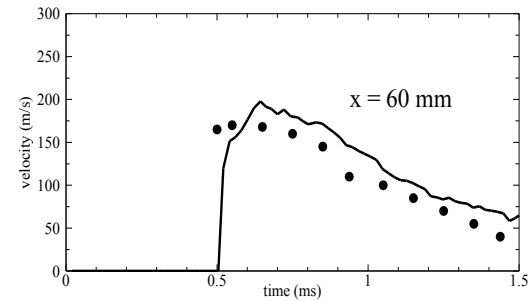
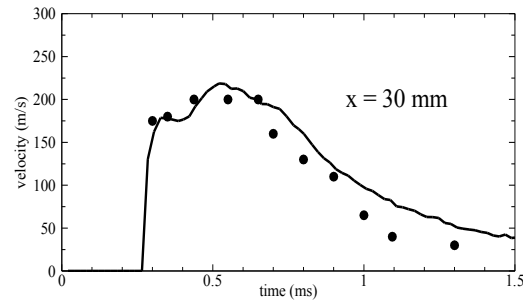
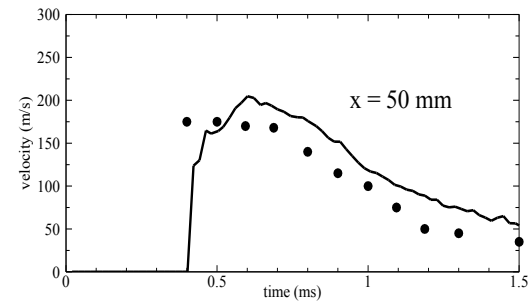
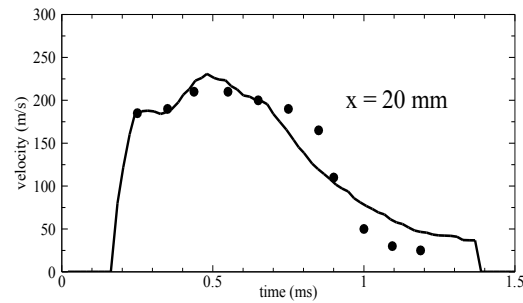
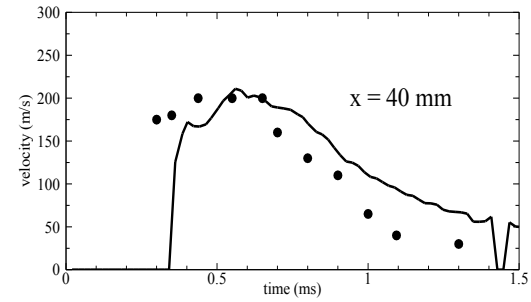
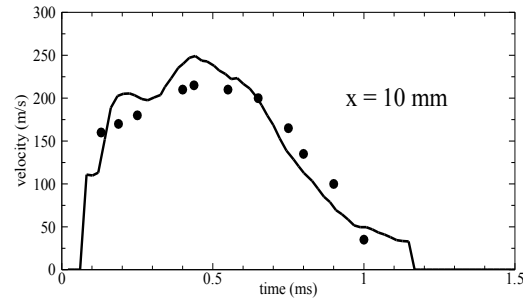
Computed mean sauter diameter.



Sauter Mean Diameter

$$D_{32} = \frac{\int_{D_{\min}}^{D_{\max}} D^3 f(D) dD}{\int_{D_{\min}}^{D_{\max}} D^2 f(D) dD}$$

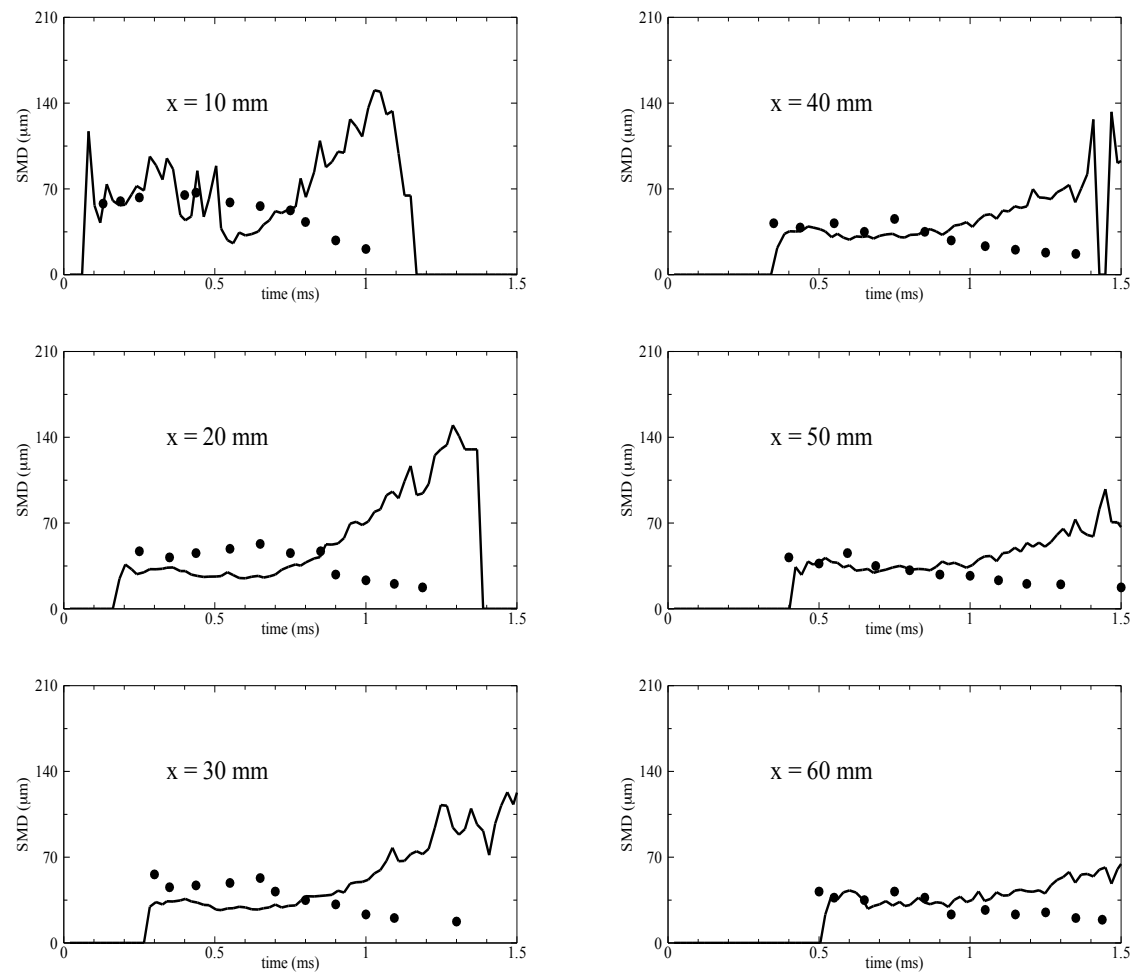
Centerline droplet mean axial velocity.



Symbols = experiment

Line = simulation

Centerline Sauter Mean Diameter (SMD).



Symbols = experiment

Line = simulation

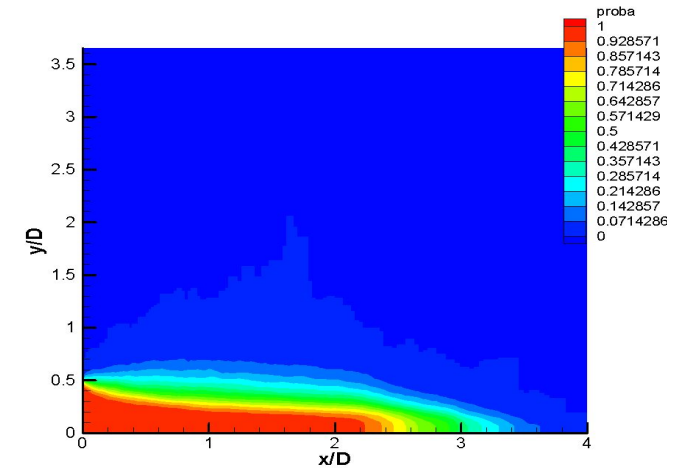
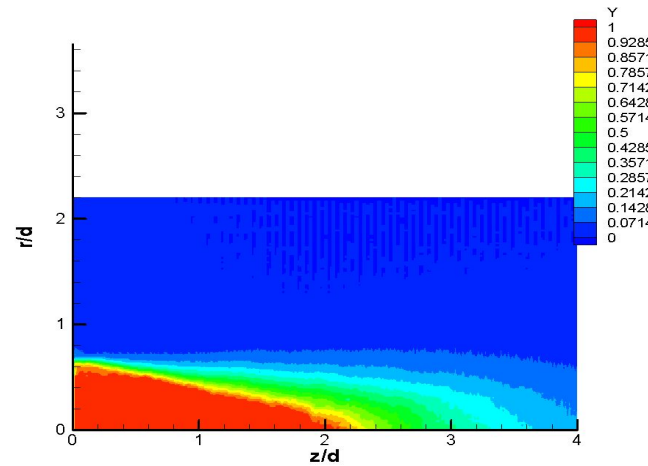
Application to Air-Blast atomization.

Experiment => mean liquid volume fraction (Stepowski & Werquin 2001)

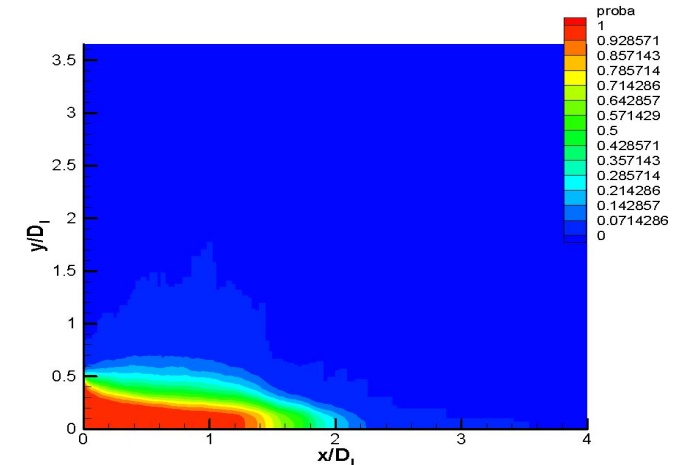
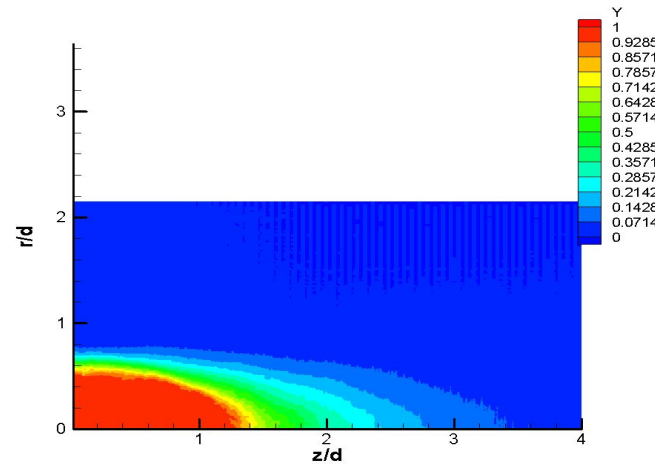
Simulation => statistics of liquid core boundary

Key parameter: $M = \frac{\rho_g u_g^2}{\rho_l u_l^2}$

$U_g = 60 \text{ m/s}, U_l = 1.36 \text{ m/s}$



$U_g = 60 \text{ m/s}, U_l = 0.68 \text{ m/s}$



Drop injection and lagrangian tracking.

Typical size resulting from
primary atomization

$$r_{typ} = \frac{1}{2} \left(\frac{\sigma}{\rho_g} We_{cr} \right)^{\frac{3}{5}} \epsilon^{-2/5}$$

Motion of the drops injected.

Lagrangian tracking :

$$\frac{dx_p}{dt} = u_p$$

$$\frac{du_p}{dt} = \frac{f}{St_p} (\langle u_g \rangle_l - u_p)$$

$f \rightarrow$ Drag coefficient , $St_p \rightarrow$ particle Stokes number

Modification of the gas velocity field:

$$\langle u_g \rangle_l = u_g (1 - P) + u_l P$$

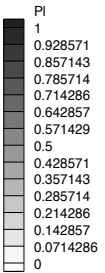
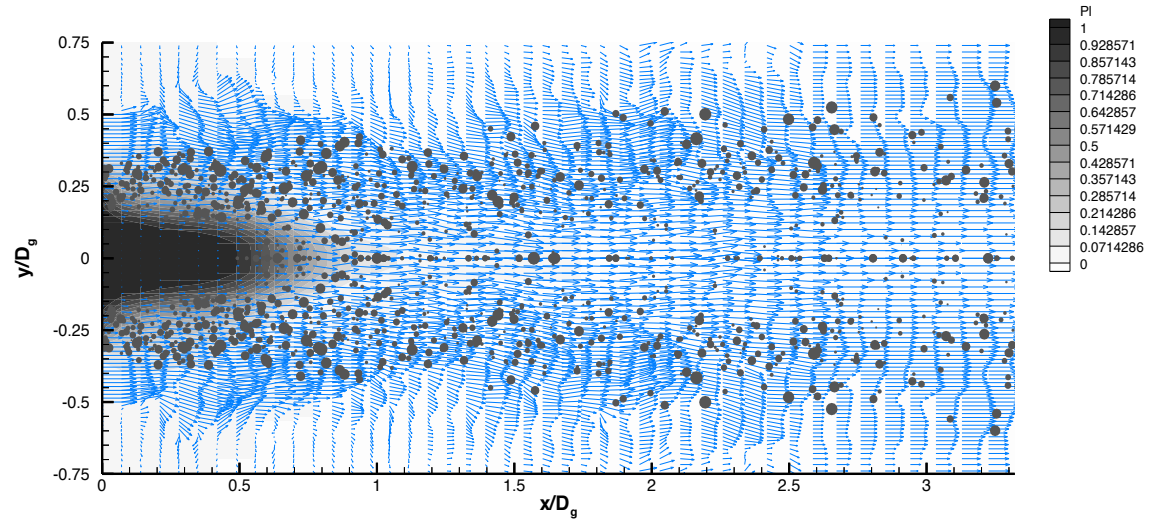
$P_l \rightarrow$ probability of presence of liquid

Distribution of formed blobs.

Experiments (Lasheras & al 1998)

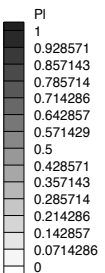
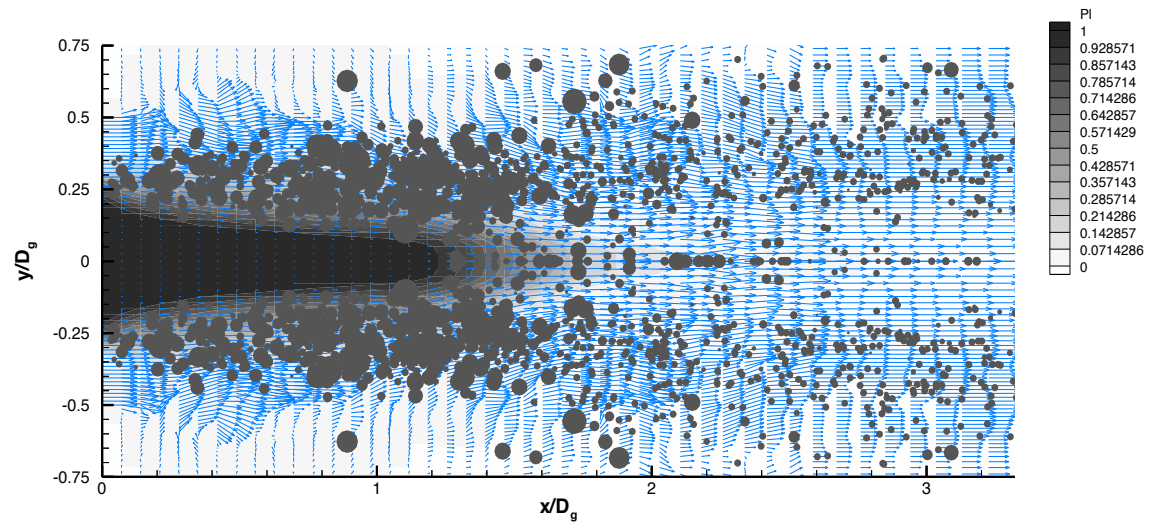
$U_g = 140$ m/s

$U_l = 0.13$ m/s



Examples of instantaneous distribution of formed droplets with instantaneous conditioned velocity of gaz and liquid core

$U_l = 2.8$ m/s

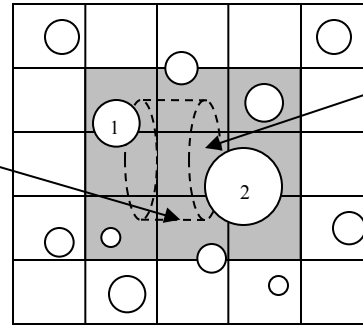


Computation in the far field.

=> Secondary processes:

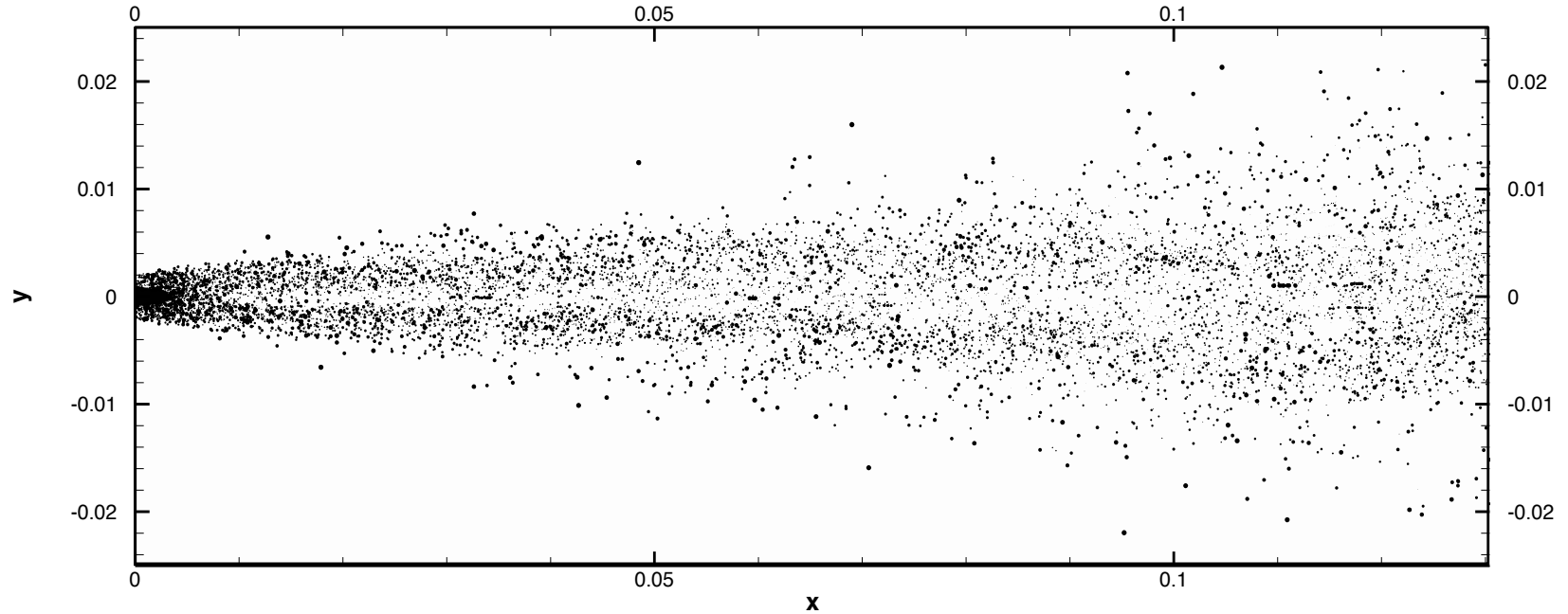
- Shearing
- Turbulence
- Collisions

$$|\vec{V}_{rel}| \delta t$$



$$S_{eff} = \pi(r_1 + r_2)^2$$

Fragmentation
or
coalescence

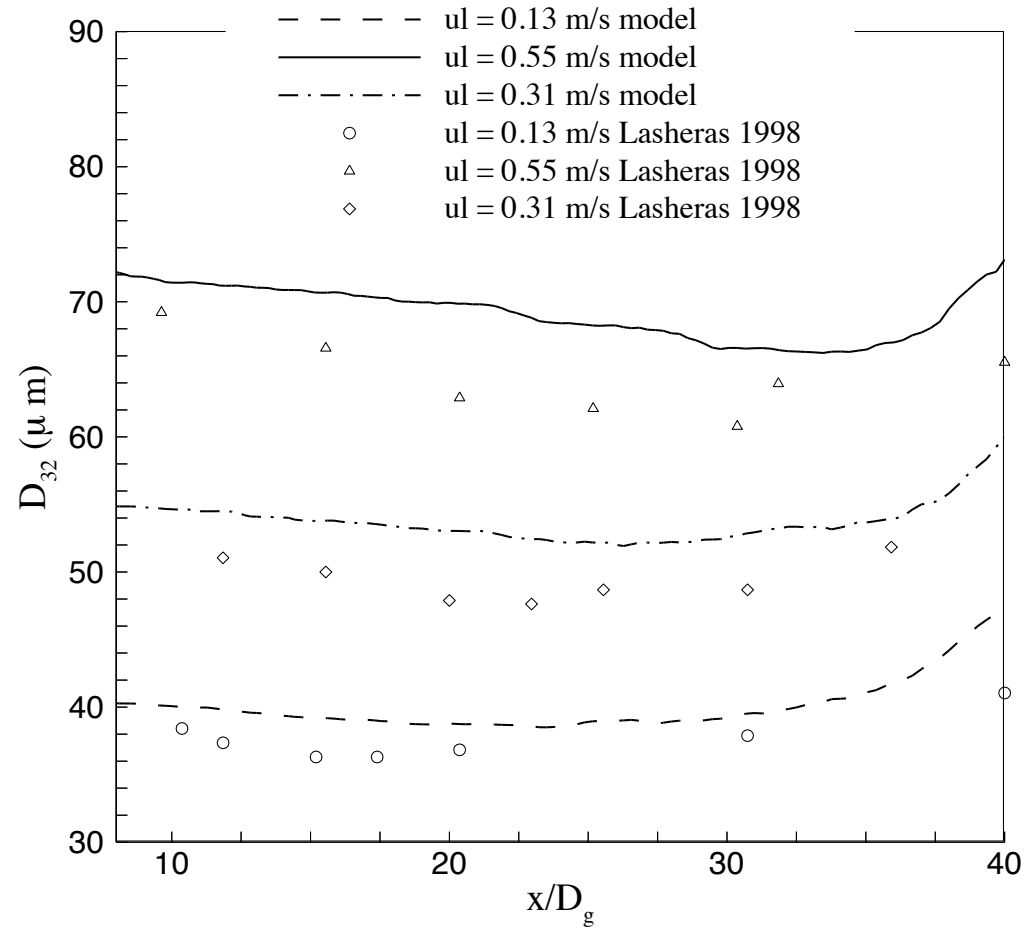


Example of instantaneous distribution of formed droplets

$u_g = 140 \text{ m/s}$, $u_l = 0.55 \text{ m/s}$

Comparison in the far field.

$U_g = 140 \text{ m/s}$



Conclusion.

- ⇒ Simple engineering model for primary atomization is proposed.
- ⇒ This allows to form the blobs in the near-injector region.

Future work.

- ⇒ Comparison with experiments in Brighton (trying different main mechanisms for fragmentation).